Virtual Reality Visualization of 3-D Electromagnetic Fields

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Abstract

One of the major problems in three-dimensional (3-D) electromagnetic field computation is visualizing the calculated field. Virtual reality techniques can be used as an aid to this process by providing multiple viewpoints, allowing immersion within the field, and taking advantage of the human ability to process 3-D spatial information. In this paper we present an example of 3-D electromagnetic field visualization in the CAVE virtual-reality environment.

1   Introduction

Electromagnetic field analysis and design are more difficult in three dimensions than in two. Not only is the mathematics more complex (multiple-valued scalar potentials, gauge conditions on vector potentials), but so are the visualization aspects. The complexity arises from the greater amount of data (more mesh points, more field components per mesh point) and the desire to view the computational mesh and electromagnetic field calculations together.

Scientific visualization of three-dimensional (3-D) vector fields, such as electromagnetic fields, has been accomplished with a number of techniques [2]. The simplest of these is to place an *icon* within the data field to express local characteristics of the field. The icon can be an arrow plot or probe [4]. An arrow is a line segment whose length is proportional to the magnitude of the vector and whose orientation depicts the vector's direction. A probe is a set of graphic primitives expressing a number of local characteristics such as curvature and torsion.

Global characteristics of the 3-D vector field can be expressed by watching a particle as it is "dropped" and advanced through the field. The resulting *streamline* traces out the path that a massless particle would take through the field, with every point on the streamline tangent to the vector field. Two or more particles advanced through the field can sweep out a surface or ribbon.

A *streamsurface* consists of many individual particles that combine particle and surface techniques [9]. Each particle is modeled as a small part of a surface. The resulting surface can

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express global characteristics such as gradual twist in the field. Particles rendered on the surface can express more local characteristics, such as velocity, for example by blurring the particle if the velocity in that area is large.

Volume visualization can also be used to visualize vector fields. An isosurface is generated by defining a function that interprets vector values into scalar values, such as magnitude for electromagnetic fields [11]. All points that are above (below) a specified scalar value generate a surface.

Although such techniques are widely used, limitations still exist. These include being able to view the field only from a single location and orientation, not seeing the entire data set at once, and trying to visualize a 3-D quantity with two-dimensional techniques. Virtual reality (VR) allows new ways to visualize electromagnetic fields that overcome these limitations.

To show the promise of VR techniques for 3-D electromagnetic field visualization, we discuss the use of VR to visualize the magnetic field of an accelerator magnet. VR can be particularly useful in the design phase of such magnets, which is complicated by the three-dimensional aspects of the problem, the variety of design parameters that exist, and the amount of computation time involved in parametric design studies.

2   Virtual Reality

A virtual reality system provides immersion and interactivity. *Immersion* is achieved through visual and audio cues. Visual cues include wide field of view, stereo display, and viewer-centered perspective. Audio cues include localized sound and synthesized sound. *Interactivity* refers to the real-time involvement the user must have with the perceived environment.

Virtual reality strives to be a natural user interface. It allows the scientist to focus the data, rather than the computer interface [5]. The objective is an environment that our senses are accustomed to and process well, in particular, 3-D spatial information [6].

A variety of technologies exist to enable virtual environments. Visual displays are implemented with cathode ray tube (CRT) or liquid crystal display technology. These displays can be free standing or placed on head-mounted units. CRTs are also used to project onto large screens. Correct stereoscopic images are sent to the viewer's eyes by using two displays, one for each eye, or by using one display with shuttered or polarized glasses. The viewer's position and movements are tracked by magnetic or ultrasonic sensors [1]. Control devices include the dataglove and the force-feedback joystick [6].

The CAVE[1] (CAVE Automatic Virtual Environment) [3] is the virtual reality system we used. The CAVE is a three-meter cube in which the user is surrounded by stereoscopic computer images rendered on the walls and floor. Left- and right-eye views are computed 48 times per second for each eye. A person standing inside the CAVE wears LCD shutter glasses that synchronize the left and right eye views, giving the illusion of three-dimensional immersion. The user is tracked by an electromagnetic tracking system, so that his or her instantaneous position and orientation are known. This system allows the environment to be rendered in correct viewer-

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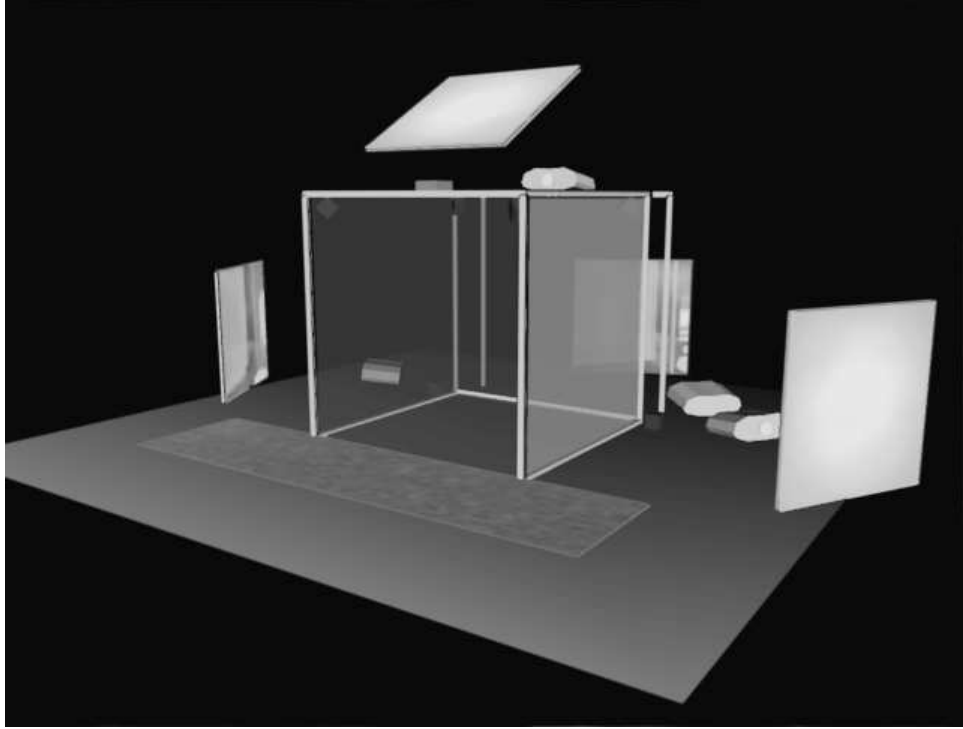[1]The Cave and ImmersaDesk are trademarks of the Board of Trustees at the University of Illinois

Figure 1: The CAVE virtual reality environment. Computer images sent to the projectors are folded by the mirrors and directed onto the CAVE walls and floor.

centered perspective. The CAVE resolution is 1024×760 pixels.

The user is able to manipulate objects within the CAVE by using a wand, a three-dimensional analog of the mouse of current computer workstations. The CAVE allows multiple users to share the virtual environment by donning a pair of shutter glasses and stepping into the cube structure. Figure 1 is a picture of the CAVE environment.

CAVE applications are typically written in C or C++ and rely upon a library of CAVE system calls to easily integrate the program into the virtual reality environment. The CAVE library manages the computation of user-centered perspective, synchronization of frames across the walls, and tracking and wand I/O.

3   Accelerator Magnet Case Study

As an example of the use of virtual-reality for 3-D electromagnetic field visualization, we use an accelerator magnet from the Advanced Photon Source (APS) at Argonne National Laboratory. The APS is a synchrotron radiation facility that, when completed, will produce extremely brilliant x-ray beams that will allow scientists to study smaller samples, more complex systems, and faster reactions and processes than ever before.

The x-rays are produced by accelerating a positron (positively charged electron) beam that orbits the APS storage ring with an energy of seven billion electron volts. Special arrays of
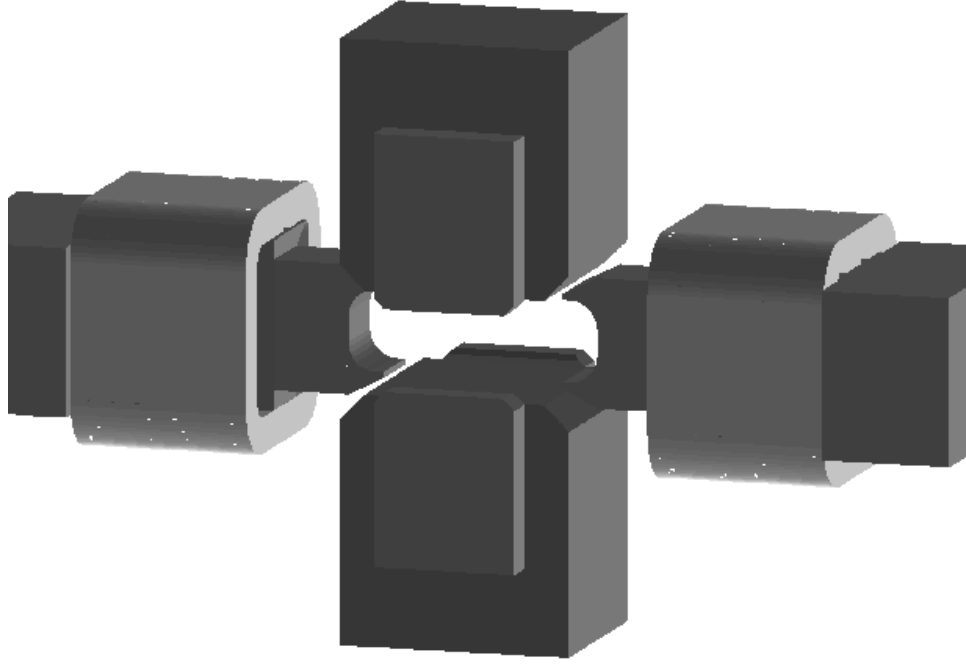
Figure 2: One half-period of the elliptical multipole wiggler magnet. One pair of poles and coils for the electromagnet is shown on the left and right. One pair of permanent magnets is on the top and bottom. One pair of half-poles for the hybrid magnets is at the front, and another pair is at the back. Note that the hybrid-magnet poles and electromagnetic poles are a quarter-period apart.

magnets, called insertion devices, manipulate the positron beam in order to fix its energy and increase its brilliance. One such device is a wiggler magnet. In a *wiggler* magnet, the magnetic field periodically alternates in direction. The transverse acceleration of the positrons by this alternating field produces the x-radiation. Wiggler magnets produce very intense, but incoherent, radiation over a wide range of energies. The particular design of a wiggler magnet determines the brightness and spectrum of the x-ray radiation emitted. These tuned x-ray beams are then further processed by optical instrumentation before they strike the sample being studied.

The subject of our work was the visualization of the magnetic field of the elliptical multipole wiggler magnet (EMW) [8]. The EMW combines an electromagnet providing a horizontal field with a hybrid magnet providing a vertical field. (In a hybrid magnet, permanent magnet material generates the field, and steel poles shape it.) The poles of the two series of magnets are 90 degrees apart, so that the field from the hybrid magnet is strongest where the field from the electromagnet is zero, and vice versa.

Figure 2 shows a single half-period of the EMW and extends from the center of one pair of hybrid magnet poles at the front to the next at the back. The poles are joined by one pair of permanent magnets at the top and bottom. Halfway between the poles of the hybrid magnets are a pair of poles and coils for the electromagnets on the left and right. The vertical pole gap is 24 mm, and the horizontal pole gap is 71 mm. The peak vertical field is 0.9 T, and the peak horizontal field is 0.1 T. The full EMW magnet is an array consisting of a total of 18 periods.
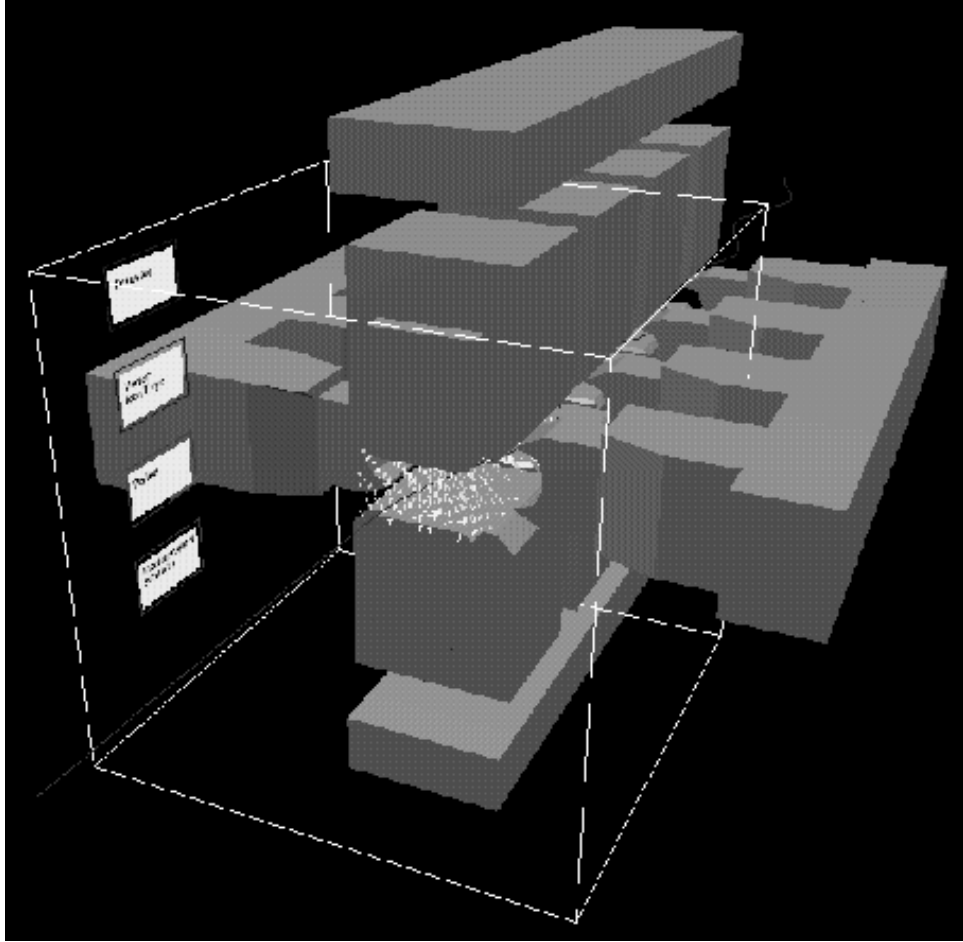
Figure 3: Four half-periods of the EMW displayed in the CAVE simulator

4 Virtual Reality Implementation

Our CAVE simulation depicts the magnet geometry, the field pattern from the combined magnets, and the trajectory of the positron beam traversing the EMW. The user interacts with the simulation as described below.

4.1 Magnet and Field Display

The visualization displays (up to) four half-periods of the EMW magnet geometry and the calculated magnetic field. The field computations were carried out using the 3-D magnetostatics program TOSCA [10], and the magnet geometry was reconstructed from an OPERA [10] data set with the code CORAL [7]. The geometry of the magnet gives the physical context in which to display the calculated magnetic field. Figure 3 from the CAVE simulator shows an "outside looking in" view of four half-periods of the EMW magnet.

The magnetic field is displayed in the interior of the EMW on a 3-D grid of points. An icon (either a cone or a cylindrical bar) is used to represent the magnet field value. The icon is
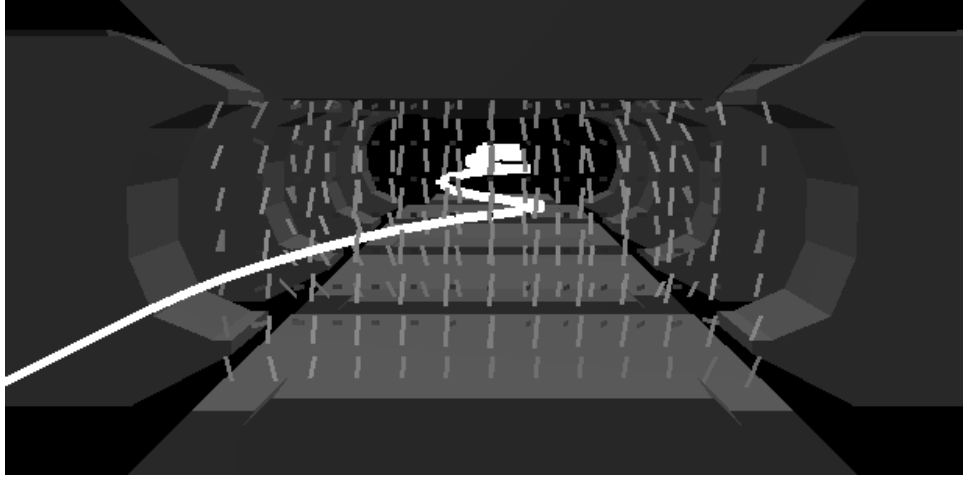
Figure 4: Path of the positron beam displayed in the CAVE simulator

oriented in the direction of the magnetic field at that point in space. The icon's color and size are a function of the vector's magnitude at that point.

A compile-time parameter allows the user to specify the number of icons used to display the magnetic field. This capability can be useful when there are many 3-D grid points and the number of icons overwhelms the user's ability to comprehend the results. For a similar reason, we display only one half-period of the magnetic field, irrespective of the number of half periods of the magnet that are displayed.

4.2   Beam Trajectory

The particle beam trajectory through the EMW magnetic field was calculated and then displayed during the simulation. The positrons move in a helical path controlled by the strength of the current in the coils of the electromagnet. A tracer sphere dynamically follows the calculated trajectory. At the maximum/minimum excursion in the horizontal plane (which occurs when the beam passes through the permanent magnet poles), the simulation displays a flash to indicate that x-ray energy is emitted.

Figure 4 shows the path of the positron beam through the magnetic field in the CAVE simulator. The trajectory is a flattened helix because the vertical field is 0.9 T and the horizontal field is only 0.1 T. When displaying the trajectory we use a scale factor in the horizontal and vertical directions to enhance the visibility of the beam. The trajectory is not scaled in the beam direction. The scale factor is large because the transverse displacements are on a micron scale.

4.3   Interactive Use

Six options are available for interacting with the simulation in the CAVE. These options are provided via a 3-D interface: a menu displayed on the left wall of the CAVE. The wand is used

to select the desired menu item.

The first option toggles the icon used to represent the magnetic field between the cones and cylindrical bars. The next two menu items allow the user to displace or rotate the complete simulation, respectively. Although the user's position and orientation in the CAVE are known, thereby allowing the environment to be rendered in correct viewer-centered perspective, we found it advantageous to be able to use the wand to enable/disable additional translation and/or rotation of the magnet geometry. By using the wand for translation, one can push or pull the magnet and field to a desired location for viewing without "walking into" one of the CAVE walls. Similarly, the wand allows for easy 360 degree rotation about the vertical axis.

The fourth option allows the user to specify the number of half-periods of the EMW magnet to display. There are 18 full periods in the EMW array. However, since the field is periodic, and displaying all 18 periods would overwhelm the user with data, we limit to four the maximum number of half-periods displayed. If the user chooses to display zero half-periods the magnetic field is shown without the context of the magnet's geometry.

The fifth option toggles the display of the particle that traces the positron beam's trajectory. The beam trajectory and displayed field can be changed by the sixth option, the magnitude of a scale factor for the current in the electromagnet. The scale factor simulates the increase in current in the electromagnet, leading to a horizontal field of up to 1.0 T. This option intuitively demonstrates to the user the relationship between the electromagnet's field strength and the (approximated) changes in orientation and magnitude of the resulting vector field and beam trajectory.

5   Discussion

We found that virtual-reality provides a new way to view 3-D electromagnetic field calculations. In contrast to traditional plane-at-a-time or 2-D mappings of 3-D data, the user obtains a panoramic view of the field. He or she may move freely about the virtual environment and explore the electromagnetic field from many different angles. By changing viewpoint, one can easily overcome the effect of obstructions to visualize the geometry and field patterns.

Compared with viewing the field data externally, the CAVE allowed us to "step into the field" and view the field from the inside out. This view provided a strong sense of immersion and participation that increased our level of understanding of the field generated by the EMW magnet. This intuitive understanding is often difficult to achieve through conventional scientific visualization.

An important advantage of the CAVE environment is that multiple users can simultaneously share the virtual experience. In our case, both the magnet designer and end user of the electromagnetic field can observe the field behavior and positron orbit as, for example, the electromagnet current varies. This mode of collaboration can allow a large part of the design and testing of an electromagnetic device to be done in a virtual environment before costly physical prototypes are constructed.

Several possibilities for future enhancements exist. These include representing the magnetic

field with flux lines or flux tubes, using cutting planes of arbitrary orientation to show field variation, and varying the starting position and angle of the positron beam to explore the edge effects felt as it enters the field of the wiggler magnet.

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