ADIFOR 2.0 Users' Guide (Revision D)

by

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Chapter 1

Miscellany

1.1 Supported Systems

ADIFOR 2.0 currently runs on SPARC's running SunOS 4.1 or SunOS 5.x (Solaris 2.x), IBM RS/6000's running AIX 3.2.5 or 4.1.1, SGI workstations running IRIX Release 6.2, HP workstations running HP-UX 9.x, and x86-class personal computers running Linux, Windows 95 or Windows NT. ADIFOR 2.0 will be ported to additional computing platforms if we find sufficient interest and have access to that platform.

1.2 How to Get ADIFOR 2.0

To retrieve the ADIFOR 2.0 automatic differentiation software for educational and non-profit research use, and for commercial evaluation, visit either of the ADIFOR group World Wide Web home pages, at URL's: http://www.mcs.anl.gov/adifor, or http://www.cs.rice.edu/~adifor. These pages describe how to request access to ADIFOR 2.0 and how to download the software. The pages also contain links to publications related to ADIFOR, including many of the papers referenced in this user's guide, as well as the most recent version of this user's guide.

1.3 Legal Notices

Copyright on the ADIFOR Preprocessor is held by Rice University. Copyright on the ADIntrinsics system and the SparsLinC libraries is held by the University of Chicago.

ADIFOR 2.0 was prepared as an account of work sponsored by an agency of the United States Government, Rice University, and the University of Chicago. NEITHER THE AUTHOR(S), THE UNITED STATES GOVERNMENT NOR ANY AGENCY THEREOF, NOR RICE UNIVERSITY, NOR THE UNIVERSITY OF CHICAGO, INCLUDING ANY OF THEIR EMPLOYEES OR OF-FICERS, MAKES ANY WARRANTY, EXPRESS OR IMPLIED, OR ASSUMES ANY LEGAL LIABILITY OR RESPONSIBILITY FOR THE ACCURACY, COMPLETENESS, OR USEFUL-NESS OF ANY INFORMATION OR PROCESS DISCLOSED, OR REPRESENTS THAT ITS USE WOULD NOT INFRINGE PRIVATELY OWNED RIGHTS.

If ADIFOR 2.0 has been installed at your site in the usual manner, then a copy of the public license for ADIFOR 2.0 can be found in **\$AD_HOME/LICENSE**. The license is also available at both of the World Wide Web sites listed in Section 1.2.

Any entity desiring permission to incorporate this software or a work based on the software into commercial products or otherwise use it for commercial purposes should contact:

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Chapter 2

Some Preliminaries

Automatic differentiation is a technique for computing the derivatives of functions described by computer programs. See [18, 24] for an introduction to automatic differentiation. ADIFOR implements automatic differentiation by transforming a collection of FORTRAN 77 subroutines that compute a function f into new FORTRAN 77 subroutines that compute the derivatives of the outputs of fwith respect to a specified set of inputs of f. This paper describes step by step how to use version 2.0 (Revision D) of the ADIFOR system to generate derivative code. Familiarity with UNIX¹ and FORTRAN 77 is assumed.

We strongly suggest that you, before reading this manual, have a look at the overview papers of ADIFOR 2.0 [7] and ADIFOR 1.0 [6]. They provide an overview of the philosophy of ADIFOR, references to successful applications of ADIFOR, and a perspective of how automatic differentiation relates to other approaches for computing derivatives.

The ADIFOR 2.0 system consists of the ADIFOR Preprocessor, the ADIntrinsics template expander and library, and the SparsLinC library. The Adifor2.1 command invokes both the preprocessor and the ADIntrinsics template expander. Figure 2.1 presents a block diagram of the ADIFOR 2.0 process, which consists of three key steps:

- 1. Apply the ADIFOR Preprocessor to your FORTRAN 77 program to produce augmented code for the computation of derivatives. The preprocessor invokes the ADIntrinsics template expander directly. We refer to the machine on which you execute the preprocessor as ADI-FORHOST.
- 2. Construct a derivative driver code that invokes the generated derivative code and makes use of the computed derivatives.
- 3. Compile the generated derivative code and your derivative driver code, and link these with the derivative support packages, i.e., the ADIntrinsics exception handling package (see Appendix B), and (optionally) the SparsLinC sparse derivative package (see Appendix C). We refer to the machine on which you compile and link your derivative driver code and the ADI-FOR 2.0 support packages as EXECHOST. Notice that ADIFORHOST and EXECHOST may be different, for example, ADIFORHOST may be a SPARC workstation, and EXECHOST an RS6000.

The first step of this process can be performed on SPARC's running SunOS 4.1 or SunOS 5.x (Solaris 2.x), IBM RS/6000's running AIX 3.2.5 or 4.1.1, SGI workstations running IRIX Release 6.2, HP workstations running HP-UX 9.x, and x86-class personal computers running Linux, Windows 95

¹UNIX is a trademark of AT&T.

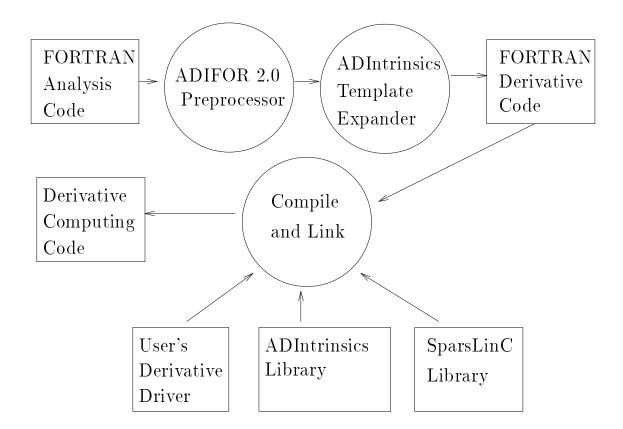


Figure 2.1. Block Diagram of the ADIFOR Process

or Windows NT. ADIFORHOST is, therefore, currently limited to be a SPARC, an IBM RS/6000 or, an SGI workstation, an HP workstation, or an x86-class personal computer. We currently provide the necessary libraries for the second step precompiled for each of the machines listed above. Source code for the libraries is also provided in case you need to compile them to execute on other architectures. A "C" compiler is required to compile the SparsLinC library. It should, therefore, be possible to use any machine as EXECHOST.

2.1 Installation

All of these files in the ADIFOR 2.0 distribution can be retrieved from the World Wide Web sites documented in Section 1.2 of this guide. The distribution consists of the following files:

- Readme.txt provides late-breaking news about the ADIFOR 2.0 distribution, including announcements of the availability of precompiled versions of the ADIFOR 2.0 executables and libraries for new architectures.
- InstallGuideUnix.txt and InstallGuideWindows.txt list the steps required to install AD-IFOR 2.0 on your system.
- ad2.0D-XXXX.tar.gz is a gzip-compressed UNIX tar format file. XXXX is one of SunOS-4.x, SunOS-5.x, AIX, IRIX, Hpux, or Linux86.
- ad20D.exe is a self-extracting installer for Windows 95 and Windows NT.

The files ad2.0D-XXXX.tar.gz and ad20D.exe unpack into two directories named ADIFOR2.0D and ADIFOR2.0D.lib.

Directory ADIFOR2.0D contains:

- bin: Contains Adifor2.1, the ADIFOR Preprocessor, and purse, the ADIntrinsics template expander. The template expander is responsible for expanding generic exception-handling macros introduced by ADIFOR 2.0 into the appropriate FORTRAN 77 code. The purse executable is a perl script.²
- templates: Contains the definition of the exception handling macros used by purse.
- docs: Contains postscript versions of relevant working notes and papers, including this manual.
- examples: Contains examples of programs processed with ADIFOR 2.0.
- man: Contains the man page for ADIFOR 2.0.
- perl_lib: Contains the perl libraries required by purse.

Directory ADIFOR2.0D.lib contains:

- src: Contains the source for the ADIntrinsics and SparsLinC libraries.
- lib: Contains the precompiled versions of the ADIntrinsics and SparsLinC libraries.
- bin: Contains several auxiliary binaries for use in building the libraries.

²We have provided executables for perl version 5 in case it is unavailable on your system. To avoid conflicts with any version of perl you have installed on your system, we have named our copies of perl to be perl- AD_DS . The purse executable invokes the copy of perl that we have provided using this name.

Machine/OS	compressed tar file
SPARC/SunOS 4.1.x	ad2.0D-SunOS-4.x.tar.gz
SPARC/SunOS 5.x (Solaris 2.x)	ad2.0D-SunOS-5.x.tar.gz
RS/6000/AIX 3.2.5 or 4.1.1	ad2.0D-AIX.tar.gz
SGI/IRIX 6.2	ad2.0D-IRIX.tar.gz
HP/HPUX 9.x	ad2.0D-Hpux.tar.gz
x86/Linux	ad2.0D-Linux86.tar.gz

Table 2.1. Machine to Archive Mapping

Machine/OS	AD_OS
SPARC/SunOS 4.1.x	SunOS-4.x
SPARC/SunOS 5.x (Solaris 2.x)	SunOS-5.x
RS/6000/AIX	AIX
SGI/IRIX	IRIX
HP/HPUX 9.x	Hpux
x86/Linux	Linux86
Cray T3E	Unicosmk

Table 2.2. Machine to AD_OS Mapping

Each UNIX tar file ad2.0D-XXXX.tar.gz contains an executable version of the ADIFOR Preprocessor for the operating system defined by XXXX. Similarly, ad20D.exe contains the Windows 95/NT executable for the preprocessor. Each of these distribution files however, contain precompiled versions of the ADIntrinsics and SparsLinC packages for all of the currently supported machines.

If you intend to run ADIFOR 2.0 on multiple kinds of machines then you will need to download and unpack several of the ad2.0D-XXXX.tar.gz or ad20D.exe files — one for each of the kinds of machine you intend to use as ADIFORHOST and EXECHOST. You may want to delete the unnecessary libraries that you get on ADIFORHOST after you unpack the tar files.

We now describe the installation and configuration procedure for ADIFOR 2.0 under Unix and Windows 95/NT.

2.1.1 Unix Installation and Configuration

To install ADIFOR 2.0 on one of the supported UNIX machines, you should first download the appropriate gzip-compressed tar file. Table 2.1 provides the names for these files. Once you have downloaded the file, you should move it into the directory in which you wish to place the ADIFOR2.0D and ADIFOR2.0D.lib directories, and then "un-gzip" and "untar" the file using the following commands:

% gunzip ad2.0D-XXXX.tar.gz % tar xf ad2.0D-XXXX.tar % gnutar zxf ad2.0D-XXXX.tar.gz

or

where XXXX is one of SunOS-4.x, SunOS-5.x, AIX, IRIX, Hpux, or Linux86.³

³ If necessary, you should download a copy of gunzip or gnutar from ftp://prep.ai.mit.edu/pub/gnu/.

To configure ADIFOR 2.0, set the environment variable AD_HOME to be the path to the directory ADIFOR2.0D, AD_LIB to be the path to the directory ADIFOR2.0D.lib, and the variable AD_OS as indicated in Table 2.2.

setenv AD_HOME /usr/local/ADIFOR2.0
setenv AD_LIB /usr/local/ADIFOR2.0.lib
setenv PATH \$AD_HOME/bin:\$PATH
setenv MANPATH \$AD_HOME/man:\$MANPATH
setenv AD_OS SunOS-4.x

Figure 2.2. Portion of .cshrc File

The directories "\$AD_HOME/bin" and "\$AD_HOME/man" should be added to your execution and manual paths, respectively. (The notation \$X represents the value of the environment variable X.) If you use csh or a variant thereof, we suggest modifying your ".cshrc" file to define AD_HOME and to modify your execution and manual paths. Figure 2.2 shows a fragment of a ".cshrc" file that has been modified assuming that ADIFORHOST and EXECHOST are the same machine, and that the ADIFOR2.0D and ADIFOR2.0D.lib directories have been installed in /usr/local on a SPARC running SunOS 4.1.3. If you are using a shell other than csh, then use the appropriate commands to modify your environment variables.

The rest of this manual assumes that you have set AD_HOME and AD_LIB and modified your execution path and manual path as just described. It is also assumed that ADIFORHOST and EXECHOST are the same machine.

To link the ADIntrinsics package into an executable under $UNIX^4$, you should use a command of the form (assuming that f77 is the Fortran 77 compiler)

```
f77 -o adnewton adnewton.o g_func.o dlange.o dgesv.o ... \
    $AD_LIB/lib/ReqADIntrinsics-$AD_OS.o \
    $AD_LIB/lib/libADIntrinsics-$AD_OS.a
```

or, equivalently,

f77 -o adnewton adnewton.o g_func.o dlange.o dgesv.o ... \
 \$AD_LIB/lib/ReqADIntrinsics-\$AD_OS.o \
 -L \$AD_LIB/lib -lADIntrinsics-\$AD_OS

Similarly, to link the SparsLinC package into an executable, use

```
f77 -o adnewton adnewton.o g_func.o dlange.o dgesv.o ... \
$AD_LIB/lib/libSparsLinC-$AD_OS.a
```

 \mathbf{or}

```
f77 -o adnewton adnewton.o g_func.o dlange.o dgesv.o ... \
    -L $AD_LIB/lib -lSparsLinC-$AD_OS
```

⁴Under IRIX on an SGI workstation, the libraries that are identified with the IRIX suffix have been compiled with the -n32 compiler flags. If you need to use -o32 or -64 compiler options, then use the libraries with suffix IRIX-o32 or IRIX-64, respectively.

2.1.2 Windows 95/NT Installation and Configuration

To install ADIFOR 2.0 on a x86-class PC running Windows 95/NT, you should download the file ad20D.exe. Executing this "self-extracting installer" will allow you to unpack all of the necessary files into a directory that you select. Do not extract the files contained in ad20D.exe into a directory whose pathname contains space characters. For example, do not attempt to install ADIFOR 2.0 into C:\Program Files\Adifor.

To configure ADIFOR 2.0 under Windows-95/NT, we suggest that you modify your autoexec.bat file to include the following commands (assuming that you have installed ADIFOR into directory C:\Adifor):

SET PATH=C:\Adifor\Adifor2.0D\bin;%PATH%; SET AD_HOME=C:\Adifor\Adifor2.0D SET AD_LIB=C:\Adifor\Adifor2.0D.lib

The Windows 95/NT version of ADIFOR 2.0 also contains the file examples.zip in the Adifor Adifor2.0D directory. You should be able to unpack these under Windows 95/NT using any modern version of "zip" on the PC.

To link the ADIntrinsics package into an executable under Windows 95/NT, you should use a command of the form:

link *.obj %AD_LIB%\lib\ReqADIntrinsics.obj \
 %AD_LIB%\lib\ADIntrinsics.lib /out:adnewton.exe

Similarly, to link the SparsLinC package into an executable, use

link *.obj %AD_LIB%\lib\SparsLinC.lib /out:adnewton.exe

2.2 Building the Libraries

It is sometimes necessary to build the ADIntrinsics and SparsLinC libraries from the source code provided. The source code for the ADIntrinsics and SparsLinC libraries are stored in subdirectories ADIntrinsics and SparsLinC of directory ADIFOR2.0D.lib/src.

The UNIX csh script Compile.Intrinsics in the ADIntrinsics directory and the csh script Compile.SparsLinC in the SparsLinC directory are used to build the libraries. To use these scripts, you will need to define a set of environment variables described in the comments at the top of each script, and then execute the script. These scripts build the libraries in the ADIntrinsics and SparsLinC subdirectories, so do not forget to copy them to the AD_LIB directory or modify the AD_LIB variable accordingly.

The Windows batch command files CompileADIntrinsics.bat and CompileSparsLinC.bat are used to build the libraries under Windows 95/NT. In contrast to the Unix scritps, these scripts copy the compiled libraries into the AD_LIB directory.

2.3 How the ADIFOR Preprocessor Transforms a Program

In this section, we describe the mechanism used by the ADIFOR Preprocessor to transform your FORTRAN 77 code into code that computes derivatives of dependent variables with respect to independent variables. The mechanism has three key subtasks: code canonicalization, variable nomination, and code generation. Understanding these three tasks will help you better understand the derivative code that is generated. We briefly describe these subtasks in the next sections.

2.3.1 Code Canonicalization

In the code canonicalization phase, the FORTRAN 77 code is rewritten into a standard form. For example, expressions appearing as arguments to function or subroutine calls and function calls appearing within conditional tests are hoisted into assignments to new temporary variables. Statement functions are expanded into in-line code. This phase also breaks up long right-hand sides of assignment statements into smaller pieces, and rewrites them such that all variables appearing on the right-hand side of an assignment statement are of the same type. The latter transformation is needed for the code to be able to link in the SparsLinC library (see Appendix C).

2.3.2 Variable Nomination

The ADIFOR Preprocessor must decide which variables need to have "directional gradient objects" or "gradient objects" associated with them. The preprocessor associates a gradient object with every variable whose value may depend on the value of a variable considered "independent" with respect to differentiation, and whose value impacts a variable considered "dependent" with respect to differentiation. Such a variable is called *active*. Variables that do not require derivative information are called *passive*.

The ADIFOR Preprocessor employs interprocedural analysis techniques to determine which variables in your code are active. First, it derives a "local interaction graph" for each subroutine. This is a bipartite graph where nodes representing input parameters or variables in common blocks are connected with nodes representing output parameters or variables in common blocks whose values they influence.

Next, an interprocedural analysis is performed, which determines, in essence, all possible program paths through which an independent variable can affect a dependent one and identifies intermediate variables that are involved along such a path. This analysis involves computing a transitive closure of the whole program graph composed from the local interaction graphs. In the presence of common blocks, equivalences, and arbitrary control structures, this is a nontrivial and computationally intensive process.

2.3.3 Code Generation

After active variables have been nominated, derivative code is generated for each assignment statement containing an active variable, and gradient objects are allocated. For assignment statements containing a FORTRAN 77 intrinsic, a template is generated that will later be instantiated by the ADIntrinsics system.

2.4 Functionality of ADIFOR 2.0-Generated Code

Consider a function func with an *n*-vector \mathbf{x} as independent and an *m*-vector \mathbf{y} as dependent variables. That is, we have

```
subroutine func(n,x,m,y)
integer n, m
real x(n), y(m)
...
end
```

The ADIFOR Preprocessor inserts a gradient object g_x for x and g_y for y (as well as gradient objects for all other active variables in func) and, in its default configuration, replaces each assignment statement in func involving an active variable with a few assignment statements and a vector loop from 1 to g_p . The interface of the routine generated from func is

```
subroutine g_func(g_p_,n,x,g_x,ldg_x,m,y,g_y,ldg_y)
integer n, m, g_p_
real x(n), y(m), g_x(ldg_x,n), g_y(ldg_y,m)
...
end
```

So, for example, $g_x(:,i)$ is the gradient object corresponding to x(i). While somewhat inconvenient, the fact that the gradient dimension is the first dimension in the gradient objects cannot be avoided if we want to be able to deal with assumed-size arrays (e.g., declared as real x(*)).

We now illustrate the flexibility inherent in the ADIFOR 2.0-generated code. First, recall the definition of the Jacobian of func,

$$J = \frac{d \ y}{d \ x} = \begin{pmatrix} \frac{\partial \ y_1}{\partial \ x_1} & \dots & \frac{\partial \ y_1}{\partial \ x_n} \\ \vdots & & \vdots \\ \frac{\partial \ y_m}{\partial \ x_1} & \dots & \frac{\partial \ y_m}{\partial \ x_n} \end{pmatrix} \in \mathbf{R}^{m \times n}.$$

Second, let $S = \mathbf{g}_{\mathbf{x}}^{T}$. We refer to S as the "seed matrix." The ADIFOR-generated code computes

$$\mathbf{g}_\mathbf{y} = (\frac{\partial \, y}{\partial \, x} \times \mathbf{g}_\mathbf{x}^T)^T = (J * S)^T,$$

where the number of columns p of S corresponds to the FORTRAN 77 variable g_p_i in the generated code. Since most of the work of the derivative code is performed in the gradient loops (which range from 1 to g_p_i), the size of p has a direct impact on the runtime and storage requirements for running the derivative code.

Properly initializing S, we can then obtain:

- **Full Jacobian:** Choosing S as the $n \times n$ identity matrix, we compute the transpose of the full Jacobian J. The complexity of the resulting derivative code is O(n) times that of the original function.
- **Jacobian-Vector Product:** Choosing $S = d \in \mathbb{R}^n$, we compute the transpose of the Jacobianvector product Jd in a time that is a small multiple (typically 2-3) of the function evaluation time. Since

$$Jd = \lim_{h \to 0} \frac{func(x+hd) - func(x)}{h}$$

this interface allows us to compute directional derivatives along arbitrary directions.

Selecting Derivatives: Choosing $S = [e_5, \ldots, e_{10}, e_{13}]$, where e_i is the *i*th canonical unit vector, i.e., an *n*-vector of all zeros except for an entry of 1 in the *i*th position, we compute the transpose of the 5th through 10th, and 13th columns of J.

See Appendix A for extensive information on seed matrix initialization. In particular, it explains how to deal with several dependent and independent variables and how to exploit sparsity in the Jacobian J.

```
program main
real x, y
read *, x
call squareroot(x, y)
print *, y
end
```

Figure 2.3. A Very Simple Program (main.f)

```
subroutine squareroot(x, y)
real x, y
y = sqrt(x)
end
```

Figure 2.4. A Very Simple Subroutine (squareroot.f)

2.5 A Quick Example

We demonstrate the use of ADIFOR 2.0, using its default configurations, with the very simple program shown in Figures 2.3 and 2.4. Procedure squareroot assigns the square root of the value of variable \mathbf{x} to variable \mathbf{y} . We now show, with only limited explanation, the sequence of steps required to construct a procedure that computes the derivative of squareroot at a user-specified value of \mathbf{x} . A more detailed description of the ADIFOR 2.0 process and of the various options available in the ADIFOR Preprocessor is presented in Chapter 4.

- 1. Construct a composition simple.cmp that lists the names of all of the FORTRAN 77 source files that constitute the example program. Figure 2.5 shows the composition we construct.
- 2. Construct a script file simple.adf that tells the ADIFOR Preprocessor to differentiate the procedure named squareroot with the independent variable x and the dependent variable y, i.e., to generate code to compute the derivative $\frac{dy}{dx}$, where y is computed from x by procedure squareroot. The script file is shown in Figure 2.6.
- 3. Create, in g_squareroot.f file in the output_files subdirectory, the procedure g_squareroot, as shown in Figure 2.7, by executing the command

Adifor2.1 AD_SCRIPT=simple.adf.

Note that an exception handler (ehufSV) is invoked when sqrt is invoked with a zero argument, as the derivative of $\sqrt{}$ is undefined. The ADIFOR Preprocessor also creates a file called

main.f squareroot.f

Figure 2.5. Script File (simple.cmp) for Simple Example

AD_TOP = squareroot AD_PMAX = 1 AD_IVARS = x AD_DVARS = y AD_PROG = simple.cmp

Figure 2.6. Script File (simple.adf) for Simple Example

```
subroutine g_squareroot(g_p_, x, g_x, ldg_x, y, g_y, ldg_y)
       real x, y
       integer g_pmax_
       parameter (g_pmax_ = 1)
       integer g_i_, g_p_, ldg_y, ldg_x
       real r1_p, r2_v, g_y(ldg_y), g_x(ldg_x)
       integer g_ehfid
       data g_ehfid /0/
       if (g_p_ .gt. g_pmax_) then
         print *, 'Parameter g_p_ is greater than g_pmax_'
         stop
       endif
       r2_v = sqrt(x)
       if ( x .gt. 0.0e0 ) then
          r1_p = 1.0e0 / (2.0e0 * r2_v)
       else
          call ehufSV (9, x, r2_v, r1_p, 'g_squareroot.f', 37)
       endif
       do g_i = 1, g_p
         g_y(g_i) = r1_p * g_x(g_i)
       enddo
       y = r2_v
C-
       ____
  _ _ _ _
      end
```

Figure 2.7. Derivative Code (g_squareroot.f)

```
program driver
real x,y
real g_x(1), g_y(1)
read *, x
g_x(1) = 1.0
call g_squareroot(1, x, g_x, 1, y, g_y, 1)
call ehrpt
print *, y
print *, g_y(1)
end
```

Figure 2.8. Derivative Code Driver (driver.f) for Simple Example

Figure 2.9. Commands to Compile and Link Derivative Code Executable

g_squareroot.A in the output_files subdirectory, which differs from g_squareroot.f only inasmuch as the code for the intrinsics exception handling has not been instantiated yet. Usually, there is no need for the user to look at the .A files. Appendix B describes this issue in more detail.

- 4. Create the derivative code driver **driver.f** as shown in Figure 2.8. The driver invokes **g_squareroot** with a user-specified value of **x** to compute the value of **y** and $\frac{dy}{dx}$. The call to the error handler reporting routine **ehrpt** produces a summary report on FORTRAN 77 intrinsics that were invoked at points of nondifferentiability (see Appendix B for details).
- 5. Compile and link driver.f, g_squareroot.f and the ADIntrinsics exception handling libraries using the commands shown in Figure 2.9 to build the desired derivative computing executable⁵

2.6 A Roadmap

The rest of this manual is organized as follows:

Chapter 3 describes how to set up the inputs to the ADIFOR Preprocessor to enable it to generate derivative code. The input to the preprocessor takes the form of *option bindings* that are specified on the command line or in startup files, and *compositions*, lists of FORTRAN 77 files that constitute the program that contains the function to be differentiated.

⁵ If you should incur problems linking on a SPARC platform, you may not have the latest version of the Sun Fortran compiler installed. You should recompile the libraries from the source we provide as described in section 2.2.

- **Chapter 4** is devoted to a step-by-step description of how to process a code by using the ADIFOR Preprocessor and an explanation of how ADIFOR 2.0-generated code should be incorporated into a program.
- Chapter 5 documents the known deficiencies in the ADIFOR Preprocessor's support for FOR-TRAN 77. For each deficiency, a workaround is presented.
- **Chapter 6** explains how to use ADIFOR 2.0 in cases where the "function to be differentiated" does not have the form expected by the ADIFOR Preprocessor.
- Chapter 7 covers some of the pitfalls associated with automatic differentiation of FORTRAN 77 programs.
- Chapter 8 provides a list of problems that users of ADIFOR 2.0 may encounter.
- Chapter 9 defines all of the options to the ADIFOR Preprocessor and presents their default values.
- **Appendix A** describes seed matrix initialization, a powerful concept that provides users of ADI-FOR 2.0 significant control over the computation performed by the generated derivative code, and allows one to compute arbitrary directional derivatives.
- Appendix B describes the ADIntrinsics template expander and library. ADIntrinsics provides user-customizable handling of exceptions within ADIFOR 2.0.
- **Appendix C** describes the SparsLinC library, which provides support for sparse derivative computations within ADIFOR 2.0.

Chapter 3

Specifying Input for the ADIFOR Preprocessor

In order to apply the ADIFOR Preprocessor to a set of FORTRAN 77 procedures to generate derivative code, it is necessary to tell it several key pieces of information:

- 1. The names of the files containing the FORTRAN 77 source code to be processed. The names of the procedures are provided to the ADIFOR Preprocessor in a file referred to as a *composition*. The preprocessor must be told the name of the file containing the composition.
- 2. The name of the "top-level routine," that routine whose invocation causes the function to be evaluated. The ADIFOR Preprocessor determines the names of all of the routines that may be transitively invoked by the top routine by examining the source code.
- 3. The names of the independent and dependent variables. The ADIFOR 2.0-generated code computes the derivatives of the dependent variables with respect to the independent ones.
- 4. Values of numerous other options to the ADIFOR Preprocessor that control how vector operations in the ADIFOR-generated code are implemented, what level of exception reporting for nondifferentiable FORTRAN 77 intrinsics is performed, and to what extent the code should be customized for particular execution environments.

The names of the composition file, the top routine, and the independent and dependent variables, and values for the various options, are provided to the ADIFOR Preprocessor in the form of bindings, as described in the next section. Section 3.2 describes the format of compositions. Section 3.3 describes source files that are acceptable for processing with the preprocessor and describes some common deviations from the FORTRAN 77 standard that cause problems.

3.1 Option Processing in the ADIFOR Preprocessor

This section describes the ADIFOR Preprocessor's option-processing mechanism. Information is provided to the preprocessor as bindings. Bindings have the form

$$OPTION = VALUE$$
,

or

$\texttt{OPTION} = \texttt{VALUE1}, \dots, \texttt{VALUEN}.$

```
AD_PROG = rosenbrock.cmp
AD_TOP = func
AD_IVARS = x
AD_DVARS = y
AD_PMAX = 2  # x has 2 elements
AD_OUTPUT_DIR = .
```



The second form is used in defining list-valued options. Bindings may be provided as command line arguments and, additionally, as lines in a "script" file. Bindings specified as command line arguments to the preprocessor may contain whitespace, consisting of a sequence of spaces and tabs, if they are quoted.

A script file is a sequence of lines. Blank lines are ignored. Each nonblank line contains a binding having either of the two forms shown above. All characters on a line after the comment character '#' are ignored. There is no formal requirement for the name of the script file, but our informal convention is to use the .adf extension. Bindings defined in script files may always use whitespace liberally.

All preprocessor options begin with an "AD_" prefix. Values of options are typically the names of files (AD_PROG), the name of a procedure in the program (AD_TOP), lists of names of variables in the program (AD_IVARS and AD_DVARS), integers (AD_PMAX), Boolean values (AD_DUMP_CALLGRAPH), and switches (AD_FLAVOR and AD_EXCEPTION_FLAVOR). For Boolean-valued options, FALSE, false and 0 are considered to be equivalent, as are TRUE, true and 1. Section 9 documents all of the ADIFOR Preprocessor options.

The ADIFOR Preprocessor processes bindings on its command line in the order that they are listed. As bindings are processed, new bindings always override values defined by a previous binding for the same option. The option AD_SCRIPT is used to specify the name of a script file. Whenever a binding for AD_SCRIPT is encountered, the file identified as the value of AD_SCRIPT is opened, and the bindings in the file processed in order.

Relative path names specified as command line arguments to the ADIFOR Preprocessor are taken as relative to the directory in which the preprocessor was executed. Relative path names specified in bindings specified in a script file are taken as relative to the directory containing the script file.

Now consider a sequence of examples using the script file rosenbrock.adf shown in Figure 3.1.

```
• Example 1
```

```
Adifor2.1 AD_PROG=rosenbrock.cmp AD_TOP=func \
AD_DVARS=y AD_IVARS=x AD_PMAX=2 AD_OUTPUT_DIR=.
```

This command defines AD_PROG to be the filename "rosenbrock.cmp", AD_TOP to be name of the procedure "func", AD_IVARS to be the (single item) list "x", AD_DVARS to be the (single item) list "y", and AD_PMAX to be the integer value 2. ADIFOR will place derivative files in the current directory (which in UNIX is usually denoted by a dot).

• Example 2

Adifor2.1 AD_SCRIPT=rosenbrock.adf

This command defines exactly the same values for the same set of options.

• Example 3

Adifor2.1 AD_SCRIPT=rosenbrock.adf AD_PMAX=5

This command defines the exactly the same set of values for the same set of options, except for option AD_PMAX whose value is overridden with the integer value 5.

3.2 Compositions

Compositions list the names of all of the source files to be processed by the ADIFOR Preprocessor. A composition is a list of pathnames to source files with zero, one, or more pathnames per line. All characters on a line after the comment character '#' are ignored. Multiple pathnames on the same line are delimited by commas and whitespace, where whitespace is any sequence of spaces or tabs. Relative pathnames are taken to be relative to the directory containing the composition.

The name of the composition must end with a ".cmp" extension. The name of each source file must end with a ".f" suffix. Each source file listed in a composition may contain the source for one or more FORTRAN 77 routines.

A composition must be *top-complete* and *consistent*. To be top-complete, every routine that may possibly by called as a result of invoking the top routine must be included in a source file listed in the composition. To be consistent, all procedure interfaces of routines in the listed source files must agree as to the number of arguments and the types of the arguments being passed. Many programs in use today have inconsistent interfaces. Fixing the inconsistencies may take significant effort, but is usually an enlightening process, resulting in a considerably more portable program.

In addition to being top-complete and consistent, your program must not be recursive. The ADIFOR Preprocessor will complain if it encounters a recursive program and will print out the names of each of the routines that are recursive. Recursion in FORTRAN 77 programs is usually, but not always, an indication of some underlying error.

When the ADIFOR Preprocessor generates derivative code for a file somedir/foo.f, it places the generated source code into a file g_foo.f in the subdirectory identified by the option AD_DUTPUT_DIR of the directory in which the preprocessor was executed. Therefore, no two pathnames listed in a composition may have the same basename, where the basename of somedir/foo.f is taken to be foo.f. The preprocessor will complain if multiple files in your program have the same basename.

3.3 Acceptable FORTRAN 77 Source Files

The ADIFOR Preprocessor recognizes standard FORTRAN 77 syntax extended with DO-ENDDO, IMPLICIT NONE, DOUBLE COMPLEX, and INCLUDE. Variable names need not be limited to six characters. If a program uses non-standard extensions, the preprocessor will probably not accept them. In particular, the preprocessor will not accept nonstandard intrinsic or type conversion functions, such as arsin(), arcos(), and dfloat(). These should be replaced with standard functions like asin(), acos(), and dble(). In any case, for portability reasons, it is probably a good idea anyway to make sure that all code is standard-conforming. Also not accepted are system calls such as etime(). In most cases, such calls do not affect function evaluation and may be removed, commented out, or replaced with a syntactically correct but nonfunctional subroutine, prior to processing.

We strongly urge you to make sure that all of the files in your composition compile correctly and adhere to the FORTRAN 77 standard before submitting them to the ADIFOR Preprocessor for

processing. ADIFOR will complain about syntax errors, but its error messages are likely to be more cryptic. The preprocessor will also complain about problems in your source code that the typical FORTRAN 77 compiler will fail to identify, specifically, inconsistencies between callsites and the procedures they invoke, and inconsistencies between common block declarations across procedures.

For example, in the following program fragment an integer*4 array of length 3 is passed to a subroutine whose arguments were declared to be of type character*12.

```
program main
integer*4 x(3)
...
call func(x)
...
end
subroutine func(c)
character*12 c
...
end
```

The following program fragment declares common blocks to be of different length in different program units.

```
program main
call func1
call func2
...
end
subroutine func1
common /cmn/ x(10)
...
end
subroutine func2
common /cmn/ x(20)
...
end
```

The FORTRAN 77 language definition requires that each common block, other than the blank common block //, must have the same size in each procedure in which it is declared. Another violation of the FORTRAN 77 standard in this program fragment is the fact that the common block is not declared in the main program from which both subroutines are called. While this is usually not an issue, because of the nature in which global variables are implemented, unexpected things could happen if a compiler exploited the liberty of the standard.

Chapter 4

A Tutorial Example

We demonstrate the use of ADIFOR 2.0 using the simple program shown in Figures 4.1 and 4.2. It shows a simple Newton iteration being used to minimize Rosenbrock's function. The routines **DLANGE** and **DGESV** from the LAPACK package [1, 2] are used to compute the norm of **y** and to solve the linear system $\frac{dy}{dx}s = -y$. Our goal will be to replace the subroutine **fprime**, which approximates $\frac{dy}{dx}$ by using central divided differences, with an ADIFOR-generated derivative code. This complete example is provided in **\$AD_HOME/examples/newton**.

Rosenbrock's function is used only for illustrative purposes. It is not indicative of the power of ADIFOR, which has processed programs up to 150,000 lines in length, albeit using more than 200 Mb of virtual memory in the process.

Step 1: Create a Composition File

Figure 4.3 presents composition rosenbrock.cmp for the example, assuming that newton, func, and fprime have been stored into the files newton.f, func.f, and fprime.f, and that code for dlange and dgesv and all of the routines that they invoke has been located.

Since func does not invoke any other functions or subroutines, instead of tracking down all of the source code for dlange and dgesv and the routines they invoke, we are free to create a very short composition, rosenbrock-func-only.cmp as shown in Figure 4.4, that contains only func.f.

Step 2: Create an ADIFOR Script File

To compute a Jacobian for the Newton example, you must provide ADIFOR with values for the following options:

AD_PROG: The value of AD_PROG is the name of the "composition" to be processed. The name of the composition is communicated to the ADIFOR Preprocessor by specifying AD_PROG=composition-name on the command line.

In this example, AD_PROG will be set to rosenbrock.cmp.

AD_TOP: The value of AD_TOP is the name of the procedure that contains the function to be differentiated. That procedure may invoke other procedures to an arbitrary nesting level. We refer to the procedure that is invoked to evaluate the function as the *top-level routine* or **TOP**. The name of the procedure **TOP** is communicated to the ADIFOR Preprocessor by using the command line option AD_TOP=procedure-name.

```
PROGRAM NEWTON
    DOUBLE PRECISION DUMMY, TOL, DLANGE
     INTEGER INFO, N, IPIV(2)
    DOUBLE PRECISION X(2),Y(2),YPRIME(2,2)
     EXTERNAL DGESV, FPRIME, FUNC, DLANGE
    TOL = 1.0E - 12
     WRITE (*,FMT=*) 'Input 2-element starting vector '
    READ (*, FMT=*) X(1), X(2)
    CALL FUNC(X,Y)
 10 IF (DLANGE('1',2,1,Y,2,DUMMY).LT.TOL) GO TO 20
    CALL FPRIME(X,Y,YPRIME)
    Y(1) = -Y(1)
    Y(2) = -Y(2)
    CALL DGESV(2,1,YPRIME,2,IPIV,Y,2,INFO)
     X(1) = X(1) + Y(1)
    X(2) = X(2) + Y(2)
     CALL FUNC(X,Y)
     WRITE (*, FMT=1000) 'Current Function Value:', Y(1), Y(2)
    GO TO 10
 20 CONTINUE
    WRITE (*,FMT=1000) 'Minimum is approximately:',X(1),X(2)
1000 FORMAT (a,1x,2 (d15.8,2x))
    END
```

Figure 4.1. A Simple Implementation of Newton's Method

In Section 6 we will describe how to handle codes where the function to be differentiated does not conveniently correspond to a procedure invocation.

In this example, the function to be differentiated corresponds to the subroutine func, so we will set AD_TOP to be func.

AD_IVARS and AD_DVARS: The values of AD_IVARS and AD_DVARS are comma-separated lists of independent (input) and dependent (output) variables of **TOP**, respectively. AD_OVARS is a synonym for AD_DVARS. A variable may be designated as independent, dependent, or both (if it is overwritten during the execution of AD_TOP).

There is no way to nominate individual elements of a FORTRAN 77 array as being independent and dependent, although it is possible to specify at run time that only derivatives with respect to a particular set of elements should be computed (see Appendix A). Variables in the AD_IVARS and AD_DVARS lists must have type real, double precision, complex or double complex. The independent and dependent variables must be formal parameters of **TOP**, or global variables declared within **TOP**. Again, in Section 6 we will describe how to handle codes in which the variables that logically correspond to the independent and dependent variables are neither formal parameters nor global variables in **TOP**.

In this example, in order to compute the derivatives of y with respect to x, we will set AD_DVARS to y and AD_IVARS to x.

AD_PMAX: The value of AD_PMAX is the upper bound on the number of independent variables for which derivatives can be computed simultaneously. It is necessary to specify this upper bound because FORTRAN 77 does not provide a standard mechanism for dynamic memory allocation. It is introduced as the first dimension of each of the gradient objects declared

```
SUBROUTINE FUNC(X,Y)
      DOUBLE PRECISION X(2),Y(2)
      Y(1) = 10.0* (X(2)-X(1)*X(1))
      Y(2) = 1.0 - X(1)
      RETURN
      END
      SUBROUTINE FPRIME (X, Y, YPRIME)
с
c approximates derivatives of Func by central differences.
С
С
       .. Array Arguments ..
      DOUBLE PRECISION X(2), Y(2), YPRIME(2,2)
С
      .. Local Scalars ..
      DOUBLE PRECISION H
С
      .. Local Arrays ..
      DOUBLE PRECISION XH(2), YM(2), YP(2)
С
      .. External Subroutines ..
      EXTERNAL FUNC
С
       . .
      IF (X(1).EQ.0.0) THEN
           H = 1.0e-7
      ELSE
           H = X(1) * 1.0e-7
      END IF
      XH(1) = X(1) - H
      XH(2) = X(2)
      CALL FUNC(XH,YM)
      XH(1) = X(1) + H
      XH(2) = X(2)
      CALL FUNC(XH, YP)
      YPRIME(1,1) = (YP(1)-YM(1))/(2.0*H)
      \text{YPRIME}(2,1) = (\text{YP}(2) - \text{YM}(2)) / (2.0 * \text{H})
      IF (X(2).EQ.0.0) THEN
           H = 1.0e-7
      ELSE
           H = X(2) * 1.0e-7
      END IF
      XH(1) = X(1)
      XH(2) = X(2) - H
      CALL FUNC(XH,YM)
      XH(1) = X(1)
      XH(2) = X(2) + H
      CALL FUNC(XH, YP)
      \text{YPRIME}(1,2) = (\text{YP}(1) - \text{YM}(1)) / (2.0 * \text{H})
      \text{YPRIME}(2,2) = (\text{YP}(2) - \text{YM}(2)) / (2.0 * \text{H})
      RETURN
      END
```

Figure 4.2. Rosenbrock's Function and Divided-Difference Approximations of the Jacobian

newton.f
func.f
func.f
fprime.f
LAPACK routines
dlange.f dgesv.f lsame.f dlassq.f
xerbla.f dgetrf.f dgetrs.f ilaenv.f
dgetf2.f dlaswp.f
BLAS routines
dtrsm.f dgemm.f idamax.f dswap.f dscal.f dger.f

Figure 4.3. Composition for Newton's Method Example (rosenbrock.cmp)

func.f

Figure 4.4. Composition for Newton's Method Example (rosenbrock-func-only.cmp)

by the ADIFOR Preprocessor. The value of AD_PMAX is communicated by using the option AD_PMAX=integer-value.

In the Newton example, we choose to set AD_PMAX to 2, since x is an array with 2 elements and we would like to compute derivatives with respect to x(1) and x(2). In general, in the invocation of the routines generated by the ADIFOR Preprocessor, we can use any value of $g_p_$ that is not larger than AD_PMAX . This issue is explained in more depth in Appendix A. We also note that if subroutines using the same common blocks are processed separately with the preprocessor, it is essential to use the same value of AD_PMAX in both cases, as otherwise the gradient object common blocks are declared inconsistently.

AD_OUTPUT_DIR: The value of AD_OUTPUT_DIR specifies the name of the directory in which the ADI-FOR Preprocessor places the generated derivative code.

In the Newton example, we have chosen to set AD_OUTPUT_DIR to be "." so that the generated code will be placed back into the directory in which the ADIFOR Preprocessor is executed.

After determining the values for each of these options, create an ADIFOR script file containing those values as shown in Figure 4.5.

```
AD_PROG = rosenbrock.cmp
AD_TOP = func
AD_IVARS = x
AD_DVARS = y
AD_PMAX = 2  # x has 2 elements
AD_OUTPUT_DIR = .
```

Figure 4.5. Script File for Newton's Method Example (rosenbrock.adf)

```
subroutine g_func(g_p_, x, g_x, ldg_x, y, g_y, ldg_y)
        double precision x(2), y(2)
С
        integer g_pmax_
С
       parameter (g_pmax_ = 2)
        integer g_i_, g_p_, ldg_y, ldg_x
        double precision d5_b, d2_b, g_y(ldg_y, 2), g_x(ldg_x, 2)
        intrinsic dble
С
С
        if (g_pmax_ .gt. g_p_) then
         print *, 'Parameter g_pmax_ is greater than g_p_'
         stop
        endif
       d2_b = dble(10.0)
       d5_b = -d2_b * x(1) + (-d2_b) * x(1)
        do g_i = 1, g_p
         g_y(g_i, 1) = d5_b * g_x(g_i, 1) + d2_b * g_x(g_i, 2)
        enddo
       y(1) = dble(10.0) * (x(2) - x(1) * x(1))
       do g_i = 1, g_p
         g_y(g_i, 2) = -g_x(g_i, 1)
        enddo
       y(2) = 1.0d0 - x(1)
C-
       return
      end
```

Figure 4.6. The ADIFOR-generated Code for Subroutine func

Step 3: Invoke the ADIFOR Preprocessor

When executed with the command:

Adifor2.1 AD_SCRIPT=rosenbrock.adf

the ADIFOR Preprocessor creates the subdirectory AD_cache, which contains internal information created by the preprocessor. Source files generated by the preprocessor are placed in the working directory. If AD_OUTPUT_DIR had been unspecified, then the default value of output_files would have caused the generated files to be placed into the subdirectory output_files. The preprocessor emits the augmented code for procedure func into the file g_func.f, whose source is shown in Figure 4.6. Note that usually an assignment statement in the original code has been replaced by a few assignment statements and a vector loop of length g_p_. When g_p_ is moderate, or the gradient objects always dense vectors, this is an efficient representation of this vector operation. The SparsLinC library (see Appendix C) provides an alternative approach for expressing this vector operation when the gradient objects are mostly sparse vectors.

Exactly the same processing process will be performed by executing the command:

```
Adifor2.1 AD_PROG=rosenbrock.cmp AD_TOP=func \
AD_DVARS=y AD_IVARS=x AD_PMAX=2 AD_OUTPUT_DIR=.
```

but without the need to create rosenbrock.adf.

Step 4: Incorporate ADIFOR-generated Subroutine

Incorporating the ADIFOR-generated subroutine into a program to compute derivatives requires the following three steps:

1. Allocate the gradient objects in the calling module. The user should carefully check the ADIFOR-generated code to determine which variables in common blocks and which arguments to the top-level routine have been found to be active. For our small example, the declarations are

double precision g_x(PMAX,2), g_y(PMAX,2)

where PMAX is an integer constant (FORTRAN 77 PARAMETER) whose value is greater than or equal to the value of AD_PMAX. In this case, we choose to set PMAX to 2.

- 2. Initialize the seed matrix. In order to compute the Jacobian of the function defined by func, the gradient object for the independent variable \mathbf{x} should be initialized to a 2×2 identity matrix. This initialization amounts to saying that the derivative of each independent variable with respect to itself is 1.0.
- 3. Call the ADIFOR-generated top-level subroutine. The ADIFOR-generated subroutine computes *both* the function value and the value of the derivatives. So, in our example, we can replace the calls to func and fprime by a single call to g_func.

In the call to the ADIFOR-generated top-level subroutine, the parameter $g_{-p_{-}}$ should be set equal to the length of the gradient objects, and all of the ldg_{-} variables should be set equal to the leading dimension with which the corresponding gradient objects (g_{-} variables) were actually declared. Thus, for our simple example, the call would look like

call g_func(2, x, g_x, PMAX, y, g_y, PMAX)

4. Call the intrinsics error reporting routine. ehrpt provides a summary report on FOR-TRAN 77 intrinsics that have been called at points where they are not differentiable. See appendix B for details.

For our example, the new driver is shown in Figure 4.7.¹ As mentioned above, since ADIFORgenerated derivative code computes the transpose of the Jacobian, we must retranspose g_y before passing it to dgesv. Together with the subroutine func and the subroutine shown in Figure 4.6, the new program replaces the program shown in Figure 4.1.

Step 5: Compile and Link

After a suitable driver has been developed, the ADIFOR-generated code, the driver, and any other modules necessary to form a complete program should be compiled. Under UNIX, the necessary commands to compile and link an executable typically look like the following, where **f77** is the Fortran 77 compiler:

 $^{^1\}mathrm{Some}$ comments were removed to fit the program on one page.

PROGRAM ADNEWTON .. Parameters .. С INTEGER PMAX PARAMETER (PMAX=2) С .. Local Scalars .. DOUBLE PRECISION DUMMY, TEMP, TOL INTEGER INFO С .. Local Arrays .. DOUBLE PRECISION G_X(PMAX,2),G_Y(PMAX,2),X(2),Y(2) INTEGER IPIV(2) С .. External Functions .. DOUBLE PRECISION DLANGE EXTERNAL DLANGE С . . TOL = 1.0E - 12WRITE (*,FMT=*) 'Input 2-element starting vector ' READ (*, FMT=*) X(1), X(2)CALL FUNC(X,Y) 10 IF (DLANGE('1',2,1,Y,2,DUMMY).LT.TOL) GO TO 20 с c compute function and Jacobian at current iterate С $G_X(1,1) = 1.0$ $G_X(1,2) = 0.0$ $G_X(2,1) = 0.0$ $G_X(2,2) = 1.0$ CALL G_FUNC(2,X,G_X,PMAX,Y,G_Y,PMAX) С c transpose g_y с $TEMP = G_Y(2, 1)$ $G_Y(2,1) = G_Y(1,2)$ $G_Y(1,2) = TEMP$ С c solve J * s = -f and update x = x + sС Y(1) = -Y(1)Y(2) = -Y(2)CALL DGESV(2,1,G_Y,PMAX,IPIV,Y,2,INFO) X(1) = X(1) + Y(1)X(2) = X(2) + Y(2)с c compute new function value с CALL FUNC(X,Y) WRITE (*,FMT=1000) 'Current Function Value:',Y(1),Y(2) GO TO 10 20 CONTINUE WRITE (*,FMT=1000) 'Root is approximately:',X(1),X(2) CALL EHRPT 1000 FORMAT (a,1x,2 (d15.8,2x)) END

Figure 4.7. The Driver for the Newton Program Using ADIFOR-generated Code

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where the module ReqADIntrinsics-\$AD_OS.o and archive libADIntrinsics-\$AD_OS.a implement the ADIFOR 2.0 exception handling packages. If the SparsLinC package is required, then it will be necessary to link in the archive libSparsLinC-\$AD_OS.a, as well.

Under Windows 95/NT, the following commands should compile and link an executable, assuming that fl32 is the Fortran 77 compiler:

where the module ReqADIntrinsics.obj and archive ADIntrinsics.lib implement the Windows 95/NT version of the exception handler package. If the SparsLinC package is required under Windows 95/NT, then it will be necessary to link in the archive SparsLinC.lib.

See Appendix B for more information on the ADIntrinsics template expander and library. See Section 8 if you encounter linking problems on a SPARC platform.

Chapter 5

Known Deficiencies

In this section we describe several deficiencies in ADIFOR 2.0's support of full FORTRAN 77. In each case, it is relatively easy to "work around" each of these deficiencies. The ADIFOR Preprocessor flags each of these as being "not supported" any time that they are encountered.

5.1 Intrinsics Passed as Procedure Parameters

The ADIFOR Preprocessor prohibits intrinsics, such as DSIN and DCOS, from being passed as procedure parameters as shown in the standard-conforming FORTRAN 77 code:

```
subroutine bad(x0, x1)
double precision x0, x1
external integrate
intrinsic dsin
call integrate(dsin,x0, x1)
end
```

This deficiency can easily be circumvented by introducing a wrapper function for each intrinsic, which is to be passed as a procedure parameter, and by then passing that wrapper routine as the procedure parameter instead of the intrinsic. For example, the following code performs the same computation as the code shown above by using a wrapper function MYDS IN for intrinsic DS IN:

```
subroutine good(x0, x1)
double precision x0, x1
external integrate, mydsin
call integrate(mydsin, x0, x1)
end
function mydsin(x)
double precision x
intrinsic dsin
mydsin = dsin(x)
end
```

5.2 Intrinsics Overridden by External Functions

The ADIFOR Preprocessor prohibits external routines from overriding intrinsic functions as shown in the standard-conforming FORTRAN 77 code:

```
subroutine bad(x,y)
external cos
double precision x, y, cos
c call user defined function with name "cos"
y = cos(x0)
end
function cos(x)
...
end
```

Again, this deficiency can easily be circumvented by renaming the external function so that it does not collide with the name of any intrinsic function, as follows:

```
subroutine good(x,y)
external mycos
double precision x, y, mycos
y = mycos(x0)
end
function mycos(x)
...
end
```

5.3 I/O Statements That Contain Function Invocations

ADIFOR Preprocessor prohibits I/O statements, i.e., READ, WRITE, and PRINT, from invoking functions and statement functions as shown in the standard-conforming FORTRAN 77 code:

```
subroutine bad(y)
double precision y(10)
integer f
external f
read (3, 50) x, y(f(x))
50 format (...)
end
```

Modifying code that invokes functions from within I/O statements is very easy, but may change the meaning of the I/O statements in ways that require other I/O statements in the program to be changed as well. For example, the function call in the **READ** statement above can be removed from an I/O statement by rewriting the code as follows:

```
subroutine okay(y)
double precision y(10)
integer f, i
external f
read (3, 50) x
i = f(x)
read (3, 51) y(i)
50 format (...)
51 format (...)
end
```

Notice, however, that in the original code, the two elements that are read come from the same input file record, while in the new code, the two elements come from different records.

Chapter 6

Advanced Topics

Normally, the ADIFOR Preprocessor assumes that independent variables are passed into the toplevel routine **TOP**, and dependent variables are passed back out to the procedure that invoked **TOP**. Furthermore, it is assumed that the values of the independent variables will be assigned before **TOP** is invoked. "Passing" is either via procedure parameters or via global variables in common blocks. So, the normal ADIFOR 2.0 interface cannot compute derivatives of the following:

- variables that are declared and computed in the main program,
- variables that are declared locally in the top-level routine or variables declared in a routine transitively invoked by the top-level routine,
- variables that are assigned values during evaluation of AD_TOP and then overwritten, and
- variables that are initialized by a **READ** statement.

This section describes some workarounds for these situations.

6.1 Computation Is Not Encapsulated in Procedure

Consider the following example:

```
program main
read(*,*) x(1)
t= result of some computation involving x(1)
read(*,*) x(2)
y= result of some computation involving x(1) and x(2)
end
```

To extract a procedure suitable for using ADIFOR 2.0 to generate code for $\frac{\partial y}{\partial x(1)}$ and $\frac{\partial y}{\partial x(2)}$, you should rearrange the computation so that both $\mathbf{x}(1)$ and $\mathbf{x}(2)$ are initialized first, then invoke a new procedure that computes \mathbf{y} from $\mathbf{x}(1)$ and $\mathbf{x}(2)$ and then returns the value of \mathbf{y} as follows:

```
program main
read(*,*) x(1)
read(*,*) x(2)
y = compute(x(1), x(2))
end
function compute(x1, x2)
y = result of some computation involving x1 and x2
end
```

6.2 Variables Other Than Parameters and Globals in AD_TOP

Consider the following program:

```
program main
call foo(x,y)
end
subroutine foo(x,y)
a = x+1
y = x*x
b = x/2
end
```

If we want the derivative of \mathbf{y} with respect to variable \mathbf{x} , the code is appropriate as is. But, if we want the derivatives of

- y with respect to variable a,
- **b** with respect to variable **x**, or
- **b** with respect to variable **a**,

we run into a problem. Specifically, we cannot nominate a local variable of subroutine **foo** as dependent or independent, since it is not visible outside of **foo**. To avoid this problem, we make all "interesting" variables in subroutine **foo** visible through parameter passing or common blocks. For example, program MAIN could be rearranged to:

```
program main
call foo(x,y,a,b)
end
subroutine foo(x,y,a,b)
a = x+1
y = x*x
b = x/2
end
```

or, alternatively,

program main call foo(x,y) end subroutine foo(x,y) common /globals/a,b a = x+1 y = x*x b = x/2 end

An alternative to this workaround is the buddy system discussed below.

6.3 Variables That Are Overwritten

Consider the following program:

program main call foo(x,y) end subroutine foo(x,y) 10 y = x*x 20 y = y * x end

Say we want to compute the derivatives with respect to \mathbf{x} of variable \mathbf{y} at both the statement with label 10 and the statement with label 20. Nominating variable \mathbf{y} as the dependent variable, will generate code that computes only the derivative of \mathbf{y} at the statement with label 20.

In order to avoid this problem, we can expand \mathbf{y} into an array and modify the code to the code that follows:

```
program main
real y(2)
call foo(x,y)
end
subroutine foo(x,y)
real y(2)
10 y(1) = x * x
20 y(2) = y(1) * x
end
```

6.4 Variables Involved in I/O Statements

Sometimes the values of independent variables are read or computed within the active subtree (that is, within the subtree of procedures below the top-level subroutine). This procedure does not pose a problem, as long as the independent variables are parameters or global variables in AD_TOP, and I/O functions are handled properly. Unfortunately, we cannot automate the proper handling of I/O

functions involving active variables because, in general, we have no way to trace the flow of data values that are read or written to files.

Without this information, we have no way of knowing whether the gradient object for a variable that is involved in a **READ** statement should be set to 0.0 or initialized by reading in derivative values from the file system. Similarly, we have no way of knowing whether we should write the values of the gradient objects for variables involved in a **WRITE** statement to the file system. Therefore, the ADIFOR Preprocessor currently just echoes I/O statements like **READ** and **WRITE** without introducing code to initialize or propagate the derivatives of variables involved in the I/O statement. Because of the problems that this approach may cause, the preprocessor generates a warning message whenever it processes a source file that contains an I/O statement involving an active variable. The warning message is printed out to **stderr** as the code is processed, and embedded as a comment just before the suspect I/O statement.

Fortunately, in most of the cases that we have encountered, it is possible to use a scheme based on "buddy variables" to modify the original function code in a manner that makes it possible for the ADIFOR Preprocessor to generate correct derivative code in the presence of I/O of active variables. This workaround was originally suggested by Andreas Griewank.

As an example, consider trying to process the following code to compute the derivative of e at the statement with label 20 with respect to h at the statement with label 10:

```
program main
real lambda
read *, lambda
call foo(lambda)
end
subroutine foo(lambda)
real lambda, e, h
10 read *, h
e = h * lambda
20 write *, e
end
```

One approach to modifying this code would be to extract the **READ** statements in **foo** into **main**, and to convert variables **e** and **h** into parameters to **foo**. As an alternative, consider modifying the original code into the following code:

```
program main
    real lambda, hbuddy, ebuddy
    common /buddyvar/ hbuddy, ebuddy
    read *, lambda
    call foo(lambda)
    \mathbf{end}
    subroutine foo(lambda)
    real lambda, e, h, hbuddy, ebuddy
    common /buddyvar/ hbuddy, ebuddy
    h = 0
   read *, h
10
    h = h + hbuddy
    e = h * lambda
    ebuddy = e
20
    write *, e
    \operatorname{end}
```

and then nominating hbuddy as the independent variable, and ebuddy as the dependent variable. Initialization of hbuddy to 0.0 and g_hbuddy to 1.0 in the derivative driver for g_foo then results in g_ebuddy being assigned the derivative of e with respect to h. Notice that nominating hbuddy and ebuddy as the independent and dependent variables forces variables h and e to be active. Since h is assigned the value 0.0 prior to the read statement, g_h will be assigned the value 0.0. Therefore, since g_hbuddy is initialized to 1.0, g_h will be assigned the value 1.0 just after the READ, as required to compute the derivative of e with respect to h. Finally, the value of the computed derivative can be returned via the global variable g_ebuddy.

The scheme that we just described has three key components. The first component forces variables in I/O statements that depend on the independent variables and that are used to compute dependent variables to be identified as active variables. The second component forces the derivatives of variables appearing in **READ** statements to be initialized properly. Finally, the third component makes it possible to retrieve the values of the derivatives for variables that appear in **WRITE** statements.

Chapter 7

Pitfalls of Differentiating FORTRAN 77

Some operations that are allowed in FORTRAN 77 do not have any (or, at least not the expected) mathematical meaning with respect to differentiation. Among these are:

• Derivatives of integers and characters

The derivative of an integer or character is meaningless. As a consequence, if an integer is assigned a value from an active variable the integer variable does not become active. Thus, the gradient objects of any variables that depend on these integers may not have the expected values. The same holds true for characters.

• Equivalencing of variables of different types

The process of equivalencing variables that have different types such as in the following code fragment

```
real r(10)
double precision d(5)
complex z(5)
equivalence(r,d)
equivalence(r,z)
```

has no real mathematical meaning. Thus, if a program performs this operation, ADIFOR 2.0 will generate the corresponding equivalences for the gradient objects of the equivalenced variables, but they (and any gradient objects which depend on them) may have meaningless values. Note that this form of equivalencing is nonportable anyway, since its results depend heavily on the floating-point representation.

• Introducing points of nondifferentiability

Sometimes, for the sake of improving efficiency, a program tests the value of a variable to see whether a function is being evaluated at a special point in space, and then computes the value of the function based on that knowledge. For example, the following piece of code computes $y = x^4$.

```
if ((x .eq. 0.0d0) .or. (x .eq. 1.0d0)) then
    y = x
else
    t = x*x
    y = t*t
endif
```

If automatic differentiation is used to compute $\frac{dy}{dx}$, then the value of $\frac{dy}{dx}|_{x=0}$ will be 1.0 (because the statement y = x implies that $\frac{dy}{dx} = \frac{dx}{dx} = 1$) rather than the expected 0.0. Similarly, the value of $\frac{dy}{dx}|_{x=1}$ will be 1.0 rather than 4.0. This "anomaly" stems from the fact that automatic differentiation differentiates the statements executed in the course of program execution. This issue, as well as other subtle pitfalls, is discussed in [16].

Chapter 8

Potential Problems

Users may encounter several problems while trying to process programs with ADIFOR 2.0. We provide a brief explanation of each and possible solutions.

• ADIFOR 2.0 may complain about errors in the original FORTRAN 77 source code

As discussed in Section 3.3, ADIFOR 2.0 may report that errors are present in your FOR-TRAN 77 program that typical FORTRAN 77 compilers will not detect. Inconsistencies in subroutine interfaces and common blocks are the most frequently reported errors (see Section 3.3).

• ADIFOR 2.0-generated code fails to link on a SPARC

Sun changed the interface to the internal I/O routines provided in libF77.a between versions SC1.0 and SC2.0 of the f77 compilation system. The default version of the ADIntrinsics library (suffix SunOS-4.x) that we provide has been compiled using version SC2.0. Unresolved references for entries beginning with three underscores, such as __do_l_in, __do_l_out, __e_rsle, __s_rsle, and ___flushio, will be reported if you attempt to compile your source files with version SC1.0 and link against the SunOS-4.x libraries we provide. In this case, you should recompile the libraries (see section 2.2) and then link against them to build your executable.

• ADIFOR 2.0 may generate subscripted variables with more than 7 dimensions

If the source code being differentiated contains active variables that are declared as arrays with 7 dimensions, then ADIFOR 2.0, when generating dense derivative code, will insert gradient objects with 8 dimensions. FORTRAN 77 limits the number of dimensions for arrays to 7. It is unlikely that you will run into this problem, but if you do, then check your compiler to see whether it has an option that will extend its limits.

• ADIFOR 2.0 may generate variable names longer than 6 characters

ADIFOR 2.0 generates names for new variables that may be more than 6 characters long. FORTRAN 77 limits the number of characters in a name to 6, but all compilers we have worked with extend this limit. It is unlikely that you will run into this problem. If you do, then check your compiler to see whether it has an option that will extend its limits.

• ADIFOR 2.0 generates DO-ENDDO loop statements instead of introducing a labeled CONTINUE statement to end each loop

The DO-ENDDO statement is not standard FORTRAN 77, but is accepted by all compilers that we have encountered.

• Unneeded labels and CONTINUE statements appear in the ADIFOR-generated subroutines

In addition to creating new labels and CONTINUE statements, ADIFOR preserves those present in the original programs. There are two reasons for this functionality. The first reason is to ensure that any references to these labels (by a computed GOTO, for example) in the original program remain properly defined. Labels are also preserved to facilitate cross-referencing between the original and ADIFOR-generated code. If a certain algorithm is present near a particular label in the original program, it will be at the same location in the ADIFORgenerated code.

• By default, ADIFOR 2.0 inserts variables whose names contain '_' characters

Some compilers may not permit '_' characters to appear in variable names. This problem can be avoided by setting the option AD_SEP to a character other than '_'.

Chapter 9

ADIFOR Preprocessor Options

This section provides short descriptions of each of the ADIFOR Preprocessor options. Default values for options are presented within square brackets. Options that can be defined with a list of values are identified with a "*" superscript.

9.1 Mandatory Options

• AD_DVARS*

List of names of the FORTRAN 77 variables that contain the dependent variables of the function to be differentiated. Synonym for AD_DVARS.

• AD_IVARS*

List of names of the FORTRAN 77 variables that contain the independent variables of the function to be differentiated.

• AD_OVARS*

AD_OVARS is a synonym for AD_DVARS. At least one of AD_OVARS and AD_DVARS must be defined.

• AD_PMAX (MANDATORY if AD_FLAVOR is dense)

Maximum number of independent variables of the function to be differentiated. The value of this option is compiled into each of the dense derivative code files and is used as the first dimension of gradient objects for local and global variables.

• AD_PROG

Name of composition file.

• AD_TOP

Name of the top-level routine, the routine whose invocation is responsible for evaluating the function that is to be differentiated.

9.2 Other Options

• AD_ACTIVATE_ALL [0]

If AD_ACTIVATE_ALL is true, then all floating point variables will be treated as being active.

• AD_ALL_SAVED [0]

If your code assumes that all storage will be treated as static storage by your compiler, i.e., as if they had been listed in SAVE statements, then you must set AD_ALL_SAVED to true to generate correct derivative code. In this case, the ADIFOR Preprocessor will also treat all local and global variables in your program as being static variables, Many FORTRAN 77 compilers treat all local and global storage as being static, which means that variables always retain their value between invocations of procedures. Use of this option will increase the time required for the preprocessor to generate derivative code.

• AD_CACHE [AD_cache]

Name of directory in which the ADIFOR Preprocessor stores information about your program as analysis is performed. Permits incremental reanalysis of your code after changes to the source code or changes in options.

• AD_CHECK_COMPOSITION [false]

If set to true, the ADIFOR Preprocessor will check your program for syntax errors and inconsistent interfaces and then stop. Derivative code will not be generated.

• AD_DUMP_CALLGRAPH [false]

If set to true, causes the ADIFOR Preprocessor to print out a callgraph for the program.

• AD_DUMP_INTERFACE [false]

If set to **true**, then the ADIFOR Preprocessor will print out a description of each of the procedure interfaces in the program.

• AD_DUMP_INTERFACE2 [false]

If set to true, then the ADIFOR Preprocessor will print out a description of each of the procedure interfaces in the program. The output format generated using AD_DUMP_INTERFACE2 is somewhat different than that generated using AD_DUMP_INTERFACE.

• AD_EXCEPTION_FLAVOR [reportonce]

May be set to terse, verbose, counting, performance, or reportonce to control level of exception handler error reporting. See Appendix B for more information.

• AD_EXCLUDE_PROCS []

The ADIFOR Preprocessor ignores invocations of procedures listed in AD_EXCLUDE_PROCS, a comma-separated list of procedure names. Derivative code will not be generated for these procedures. Only use this option if the procedures you list are known not to impact the values of derivatives you want computed.

• AD_FLAVOR [dense]

The ADIFOR Preprocessor generates dense derivative code (i.e., expressing gradient objects loops as normal FORTRAN 77 loops) if AD_FLAVOR is set to dense, and sparse derivative code (i.e., calls to the SparsLinC library) if it is set to sparse.

• AD_NAMESHIFT_CALLED_PROCS []

The ADIFOR Preprocessor "shifts" the names of invoked procedures that appear in AD_NAMESHIFT_CALLED_PROCS, a comma-separated list of procedure names. The shifting operation appends a suffix to the name of each listed procedure that encodes the type of each of its arguments.

• AD_NAMESHIFT_DEFINED_PROCS []

The ADIFOR Preprocessor "shifts" the names of defined procedures that appear in AD_NAMESHIFT_DEFINED_PROCS, a comma-separated list of procedure names. The shifting operation appends a suffix to the name of each listed procedure that encodes the type of each of its arguments.

• AD_NO_CLEANUP [false]

If AD_NO_CLEANUP is true then the ADIFOR Preprocessor will skip its "cleanup" phase. This is useful if you want to understand the hybrid mode of automatic differentiation, and code transformation, used by ADIFOR.

• AD_NUM_RHS_VARS [5 if AD_FLAVOR is sparse, 500 if AD_FLAVOR is dense]

The ADIFOR Preprocessor transforms each assignment statement whose right-hand side expressions has more than AD_NUM_RHS_VARS into a sequence of simpler assignment statements.

• AD_OUTPUT_DIR [output_files]

Directory into which the ADIFOR Preprocessor places the augmented source code files.

• AD_PREFIX [g]

Character that serves as initial character of gradient object names and derivative computing procedure names. For example, by default, the gradient object for foo is g_foo.

• AD_SCALAR_GRADIENTS [false]

If set to **true** and **AD_FLAVOR** is "dense", then the ADIFOR Preprocessor will generate code that assumes that **g_pmax_** is 1. Executing this code provides an efficient means of generating J * v, where J is the Jacobian of the function being differentiated, and v is a vector.

• AD_SCRIPT []

Name of file containing additional definitions of bindings.

• AD_SEP [_]

Character that is used to separate components of generated variable names. If AD_SEP is changed to '\$', then the gradient object for foo will be named g\$foo.

• AD_SPARSLINC_USE_64_PTR [false]

If AD_FLAVOR is sparse, then setting AD_SPARSLINC_USE_64_PTR to true will cause the ADIFOR Preprocessor to declare derivative objects as INTEGER*8 values instead of INTEGER values. INTEGER*8 type variables should be able to contain all valid addresses on a 64-bit machine.

• AD_SUPPRESS_LDG [false]

If set to true and AD_FLAVOR is "dense", then the ADIFOR Preprocessor will generate code that assumes that all gradient objects are allocated with first dimensions set to g_pmax_. Leading dimension arguments will not be passed as parameters throughout derivative code. Use of this option may allow the generated code to be vectorized efficiently.

• AD_SUPPRESS_NUM_COLS [false]

If set to true and AD_FLAVOR is "dense", then the ADIFOR Preprocessor will generate code that assumes that g_p_ is g_pmax_, and hence does not pass g_p_ as a parameter throughout derivative code. Use of this option may allow the generated code to be vectorized efficiently.

• AD_TEMPLATE_DIR []

Specifies an additional directory in which to search for ADIntrinsic template files. Only a single additional directory may be specified. See Appendix B for more information.

Appendix A

Seed Matrix Initialization

A.1 Introduction

This appendix focuses on the proper and efficient use of ADIFOR-generated codes through detailed examination of seed matrix initialization for the following cases:

- Dense Jacobian, one independent, one dependent variable
- Dense Jacobian, multiple independent, multiple dependent variables
- Sparse Jacobian, one independent, one dependent variable
- Sparse Jacobian, two independent variables, one dependent variable
- Partially separable functions

In most of these cases, a "variable" denotes an array; thus, we shall be dealing with vector-valued functions.

Note: The examples presented in Appendix A correspond to seed matrix initialization for the default or "nonsparse" flavor of ADIFOR 2.0 (see AD_FLAVOR in Chapter 9). The differences between the sparse and nonsparse ADIFOR 2.0-generated codes, which are discussed in Appendix C, impose differences in the mechanics of seed matrix initialization in each case (see Section C.4.4 for details). Nonetheless, the general seeding ideas presented here for the nonsparse case apply equally as well to the sparse case.

A.2 Case 1: Dense Jacobian, one independent, one dependent variable

Our first example is adapted from Problem C2 in the STDTST set of test problems for stiff ODE solvers [15] and was brought to our attention by George Corliss of Marquette University. The routine FCN2 computes the right-hand side of a system of ordinary differential equations y' = yp = f(x, y) by calling a subordinate routine FCN:

```
C File: FCN2.f
SUBROUTINE FCN2(M,X,Y,YP)
INTEGER N
```

DOUBLE PRECISION X, Y(M), YP(M)

```
INTEGER ID, IWT
      DOUBLE PRECISION W(20)
      COMMON
              /STCOM5/W, IWT, N, ID
      CALL FCN(X,Y,YP)
      RETURN
      END
C File: FCN.f
      SUBROUTINE FCN(X,Y,YP)
С
      ROUTINE TO EVALUATE THE DERIVATIVE F(X,Y) CORRESPONDING TO THE
С
      DIFFERENTIAL EQUATION:
С
                    DY/DX = F(X,Y).
      THE ROUTINE STORES THE VECTOR OF DERIVATIVES IN YP(*). THE
С
С
      DIFFERENTIAL EQUATION IS SCALED BY THE WEIGHT VECTOR W(*)
      IF THIS OPTION HAS BEEN SELECTED (IF SO IT IS SIGNALLED
С
С
      BY THE FLAG IWT).
      DOUBLE PRECISION X, Y(20), YP(20)
      INTEGER
               ID, IWT, N
      DOUBLE PRECISION W(20)
                    /STCOM5/W, IWT, N, ID
      COMMON
      DOUBLE PRECISION SUM, CPARM(4), YTEMP(20)
      INTEGER
              I, IID
                    CPARM/1.D-1, 1.D0, 1.D1, 2.D1/
      DATA
      IF (IWT.LT.0) GO TO 40
      DO 20 I = 1, N
         YTEMP(I) = Y(I)
         Y(I) = Y(I) * W(I)
   20 CONTINUE
   40 IID = MOD(ID,10)
С
      ADAPTED FROM PROBLEM C2
      YP(1) = -Y(1) + 2.D0
      SUM = Y(1) * Y(1)
      DO 50 I = 2. N
         YP(I) = -10.0D0*I*Y(I) + CPARM(IID-1)*(2**I)*SUM
         SUM = SUM + Y(I) * Y(I)
   50 CONTINUE
      IF (IWT.LT.0) GO TO 680
      DO 660 I = 1, N
         YP(I) = YP(I)/W(I)
         Y(I) = YTEMP(I)
  660 CONTINUE
  680 CONTINUE
      RETURN
      END
```

Most software for the numerical solution of stiff systems of ODEs requires the user to supply a subroutine for the Jacobian of f with respect to y. Such a subroutine can easily be generated by

ADIFOR. For the purposes of automatic differentiation, the vector \mathbf{Y} is the independent variable, and the vector \mathbf{YP} is the dependent variable. Then ADIFOR produces

```
subroutine g_fcn2(g_p_, m, x, y, g_y, ldg_y, yp, g_yp, ldg_yp)
С
С
        ADIFOR: runtime gradient index
        integer g_p_
С
       ADIFOR: translation time gradient index
        integer g_pmax_
       parameter (g_pmax_ = 20)
С
        ADIFOR: gradient iteration index
        integer g_i_
С
        integer ldg_y
        integer ldg_yp
        integer n
       double precision x, y(m), yp(m)
        integer id, iwt
       double precision w(20)
       common /stcom5/ w, iwt, n, id
С
С
       ADIFOR: gradient declarations
       double precision g_y(ldg_y, m), g_yp(ldg_yp, m)
        if (g_p_ .gt. g_pmax_) then
         print *, "Parameter g_p is greater than g_pmax."
          stop
       endif
       call g_fcn(g_p_, x, y, g_y, ldg_y, yp, g_yp, ldg_yp)
       return
      end
      subroutine g_fcn(g_p_, x, y, g_y, ldg_y, yp, g_yp, ldg_yp)
С
С
       ADIFOR: runtime gradient index
        integer g_p_
С
       ADIFOR: translation time gradient index
        integer g_pmax_
       parameter (g_pmax_ = 20)
С
        ADIFOR: gradient iteration index
        integer g_i_
С
        integer ldg_y
        integer ldg_yp
С
       ROUTINE TO EVALUATE THE DERIVATIVE F(X,Y) CORRESPONDING TO THE
С
       DIFFERENTIAL EQUATION:
С
       DY/DX = F(X, Y).
С
       THE ROUTINE STORES THE VECTOR OF DERIVATIVES IN YP(*). THE
С
       DIFFERENTIAL EQUATION IS SCALED BY THE WEIGHT VECTOR W(*)
       IF THIS OPTION HAS BEEN SELECTED (IF SO IT IS SIGNALLED
С
C
       BY THE FLAG IWT).
       double precision x, y(20), yp(20)
        integer id, iwt, n
       double precision w(20)
       common /stcom5/ w, iwt, n, id
       double precision sum, cparm(4), ytemp(20)
        integer i, iid
```

```
data cparm /1.d-1, 1.d0, 1.d1, 2.d1/
С
С
        ADIFOR: gradient declarations
        double precision g_y(ldg_y, 20), g_yp(ldg_yp, 20)
        double precision g_sum(g_pmax_), g_ytemp(g_pmax_, 20)
        if (g_p_ .gt. g_pmax_) then
          print *, "Parameter g_p is greater than g_pmax."
          stop
        endif
        if (iwt .lt. 0) then
         goto 40
        endif
        do 99999, i = 1, n
С
           ytemp(i) = y(i)
          do g_i = 1, g_p
            g_ytemp(g_i, i) = g_y(g_i, i)
          enddo
          ytemp(i) = y(i)
С
           y(i) = y(i) * w(i)
          do g_i = 1, g_p
           g_y(g_i, i) = w(i) * g_y(g_i, i)
          enddo
          y(i) = y(i) * w(i)
20
          continue
99999
        continue
40
        iid = mod(id, 10)
С
        ADAPTED FROM PROBLEM C2
С
        yp(1) = -y(1) + 2.d0
        do g_i = 1, g_p
          g_yp(g_i, 1) = -g_y(g_i, 1)
        enddo
        yp(1) = -y(1) + 2.d0
С
        sum = y(1) * y(1)
        do g_i = 1, g_p
          g_sum(g_i) = y(1) * g_y(g_i, 1) + y(1) * g_y(g_i, 1)
        enddo
        sum = y(1) * y(1)
        do 99998, i = 2, n
           yp(i) = -10.0d0 * i * y(i) + cparm(iid - 1) * (2 ** i) * sum
С
          do g_i_ = 1, g_p_
            g_yp(g_i_, i) = cparm(iid - 1) * (2 ** i) * g_sum(g_i_) + -1
    *0.0d0 * i * g_y(g_i_, i)
          enddo
          yp(i) = -10.0d0 * i * y(i) + cparm(iid - 1) * (2 ** i) * sum
С
           sum = sum + y(i) * y(i)
          do g_i = 1, g_p
            g_sum(g_i) = g_sum(g_i) + y(i) * g_y(g_i, i) + y(i) * g_y
    *\,(g_{-}\,i_{-}\,,\ i\,)
          enddo
          sum = sum + y(i) * y(i)
50
          continue
99998
        continue
        if (iwt .lt. 0) then
          goto 680
        endif
```

```
do 99997, i = 1, n
С
           yp(i) = yp(i) / w(i)
         do g_i = 1, g_p
           g_yp(g_i, i) = (1 / w(i)) * g_yp(g_i, i)
          enddo
         yp(i) = yp(i) / w(i)
С
           y(i) = ytemp(i)
          do g_i = 1, g_p
           g_y(g_i, i) = g_ytemp(g_i, i)
          enddo
         y(i) = ytemp(i)
660
         continue
99997
       continue
680
       continue
       return
      end
```

The derivative objects g_y and g_yp are declared as matrices with 20 columns (since both y and yp were declared as vectors of length 20) and leading dimension ldg_y and ldg_yp, respectively. The parameter g_p denotes the actual length of the gradient objects in a call to g_fcn2. Since Fortran 77 does not allow dynamic memory allocation, derivative objects for local variables are statically allocated with leading dimension pmax, whose value was selected by the user during the invocation of ADIFOR. A variable and its associated derivative object are treated in the same fashion; that is, if x is a function parameter, so is g_x. Derivative objects corresponding to locally declared variables or variables in common blocks are declared locally or in common blocks as well.

Subroutine g_fcn2 relates to the Jacobian

$$J_{yp} = \begin{pmatrix} \frac{\partial yp_1}{\partial Y_1} & \cdots & \frac{\partial yp_1}{\partial Y_m} \\ \vdots & & \vdots \\ \frac{\partial yp_m}{\partial Y_1} & \cdots & \frac{\partial yp_m}{\partial Y_m} \end{pmatrix}$$

as follows: Given input values for g_p_, m, x, y, g_y, ldg_y, and ldg_yp, the routine g_fcn2 computes both yp and g_yp, where

$$g_yp(1:g_p, 1:m) = (J_{yp}(g_y(1:g_p, 1:m)^T))^T$$

The superscript T denotes matrix transposition. The user must allocate g_yp and g_y with leading dimensions ldg_yp and ldg_y that are at least g_p . While the implicit transposition may seem awkward at first, this is the only way to handle assumed-size arrays (like real a(*)) in subroutine calls.

Assume that m and g_p are 20 and that ldg_y and ldg_y are at least 20. Then we can compute the derivative matrix J_{yp} simply by initializing g_y to the identity:

On exit from g_fcn2, the variable g_yp contains the transpose of the Jacobian J_{yp} . Note that for this program to work, g_fcn2 must have been generated with AD_PMAX at least 20.

Alternatively, we could have computed the Jacobian one column at a time:

```
******
* Approach 2 *
*******
     DO 10 I = 1, M
        initialize first row of G_Y to i-th unit vector
*
        DO 5 J = 1, M
            G_Y(1,J) = 0.0D
   5
        CONTINUE
        G_Y(1,I) = 1.0D0
        call ADIFOR-generated derivative code
*
*
        call g_fcn2(1, m, x, y, g_y, ldg_y, yp, g_yp, ldg_yp)
*
        store ith column of the Jacobian in ith row of Jactrans array
        DO 15 J = 1, M
            JACTRANS(I,J) = G_{YP}(1,J)
   15
        CONTINUE
   10 CONTINUE
```

Even though $g_y(i,j)$ as computed in Approach 1 equals jactrans(i,j) computed in Approach 2, the second method is significantly less efficient. This inefficiency arises from the fact that the value of yp itself is computed once in the first approach, but m times in the second approach. Thus, it is usually best to compute as large a slice of the Jacobian as memory restrictions will allow. However, in this case, $AD_PMAX = 1$ is sufficient, and, as a result, the memory requirements of the ADIFOR-generated code can be expected to be more modest, roughly 1/20th of the memory requirements of the previous code. In this fashion, the ADIFOR interface provides a mechanism for accomodating memory/runtime tradeoffs. An example of a parallel "derivative stripmining" technique based on this approach is presented in [9].

A.3 Case 2: Dense Jacobian, multiple independent and multiple dependent variables

The second example involves a code that models adiabatic flow [25], a commonly used module in chemical engineering. This code models the separation of a pressurized mixture of hydrocarbons into liquid and vapor components in a distillation column, where pressure (and, as a result, temperature) decrease. This example was communicated to us by Larry Biegler of Carnegie-Mellon University.

In its original version, the top-level subroutine

```
subroutine aifl(kf)
integer kf
```

has only one argument. All other information is passed in common blocks. For demonstration purposes, we changed the interface slightly to

```
subroutine aifl(kf,feed,pressure,liquid,vapor)
integer kf
real feed(*), pressure(*), liquid(*), vapor(*)
```

copying the values passed in those arguments into the proper common blocks in aifl. As our first example, assume that we are interested in $\frac{\partial \ liquid}{\partial \ feed}$ and $\frac{\partial \ vapor}{\partial \ feed}^{1}$. In this case, ADIFOR generates

In our example, the feed was a mixture of the hydrocarbons N-butane, N-pentane, 1-butene, cis-2-butene, trans-2-butene, and propylene, so the length of feed, liquid, and vapor was six, with feed(1) corresponding to the N-butane feed, and so on. If we set $g_p=6$ and initialize g_feed to a 6×6 identity matrix, then on exit $g_liquid(i,j)$ contains

 $\frac{\partial \text{ (component } j \text{ in liquid)}}{\partial \text{ (component } i \text{ in feed)}},$

which predicts by what amount the liquid portion of substance j will change if the feed of component i changes.

Suppose that we also wish to treat the pressure at the various inlets as being independent, and (because of the conservation law) decide not to declare "vapor" as being dependent, ADIFOR generates

subroutine g_aifl(g_p_, kf, feed, g_feed, ldg_feed,
\$ pressure, g_pressure, ldg_pressure,
\$ liquid, g_liquid, ldg_liquid, vapor)

The initialization is a little more complicated this time. Assuming that we have 3 feeds (so **pressure** has three elements), the total number of independent variables is 6 + 3 = 9. gliquid measures the sensitivity of the 6 substances with respect to changes in the 9 independent variables. Thus,

$$J_{liquid} = \left(\frac{\partial \ liquid}{\partial \ pressure}, \frac{\partial \ liquid}{\partial \ feed}\right)$$

is a 6×9 matrix. ADIFOR computes

$$\texttt{g_liquid} = \left(J_{liquid} \left(\begin{array}{c} \texttt{g_feed}^T \\ \texttt{g_pressure}^T \end{array}\right)\right)^T.$$

If we wish to compute the whole Jacobian J, then

$$\left. \begin{array}{c} \texttt{g_feed}^T \\ \texttt{g_pressure}^T \end{array} \right)$$

¹Actually, it is sufficient to compute one or the other, since, because of conservation laws, $\frac{\partial \ liquid}{\partial \ feed} + \frac{\partial \ vapor}{\partial \ feed}$ equals the identity matrix.

must be initialized to a 9×9 identity matrix. Thus, g_feed^T must contain the first six rows of a 9×9 identity matrix (since there are six variables in the feed), and $g_pressure^T$ must contain the last three rows of a 9×9 identity matrix. This configuration is achieved by initializing

A.4 Case 3: Sparse Jacobian, one independent, one dependent variable

From the previous discussion, ADIFOR may seem to be well suited for computing dense Jacobian matrices, but rather expensive for sparse Jacobians. A primary reason is that the forward mode of automatic differentiation upon which ADIFOR is mainly based (see [7]) requires roughly $g_p_$ -operations for every assignment statement in the original function. Thus, if we compute a Jacobian J with n columns by setting $g_p_ = n$, its computation will require roughly n times as many operations as the original function evaluation, independent of whether J is dense or sparse. However, it is well known [13, 17] that the number of function evaluations that are required to compute an approximation to the Jacobian by finite differences can be much less than n if J is sparse. Fortunately, the same idea can be applied to greatly reduce the running time of ADIFOR-generated derivative code as well. This section suggests a technique for exploiting sparsity in derivative computations if the sparsity pattern is known a priori. Appendix C describes the the SparsLinC library, which, in conjunction with ADIFOR 2.0, allows exploitation of sparsity without a priori knowledge, and even computes the sparsity pattern of the Jacobian as a byproduct of the derivative computation.

The idea is best understood with an example. Assume that we have a function

$$F = \begin{pmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \\ f_5 \end{pmatrix} : x \in \mathbf{R}^4 \mapsto y \in \mathbf{R}^5$$

whose Jacobian J has the following structure (symbols denote nonzeros, and zeros are not shown):

$$J = \begin{pmatrix} \bigcirc & & & \\ \bigcirc & & & \diamond \\ & \bigtriangleup & & \diamond \\ & \bigtriangleup & \Box & \\ & \bigtriangleup & \Box & \end{pmatrix}.$$

That is, the function f_1 depends only on x_1 , f_2 depends only on x_1 and x_4 , and so on. The key idea in sparse finite difference approximations is to identify *structurally orthogonal* columns j_i of J- that is, columns whose inner product is zero, independent of the value of x. In our example, columns 1

and 2 are structurally orthogonal, and so are columns 3 and 4. This means that the set of functions that depend nontrivially on x_1 , and the set of functions that depend nontrivially on x_2 are disjoint.

To exploit this structure, recall that ADIFOR (ignoring transposes) computes $J \cdot S$, where S is a matrix with g_p_ columns. For our example, setting $S = I_{4\times 4}$ will give us J at roughly four times the cost of evaluating F, but if we exploit the structural orthogonality and set

$$S = \left(\begin{array}{cc} 1 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 1 \end{array} \right),$$

the running time for the ADIFOR code is roughly halved. Note that the ADIFOR-generated code remains unchanged.

As a more realistic example, we consider the swirling flow problem, part of the MINPACK-2 test problem collection [3], which was made available to us by Jorge Moré of Argonne National Laboratory. Here we solve a nonlinear system of equations F(x) = 0 for $F : \mathbb{R}^n \to \mathbb{R}^n$. The swirling flow code has the form

Like all codes in the MINPACK-2 test collection, it is set up to compute the function values (in fvec) and, if desired, the analytic first-order derivatives (in fjac) as well. The vectors \mathbf{x} and fvec are of size $\mathbf{nxmax} = \mathbf{14*nint}$. For example, for $\mathbf{nint} = 4$, the Jacobian of F is of size $\mathbf{nxmax} = 56$ and has the structure shown in Figure A.1.

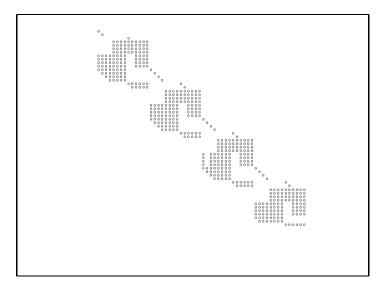
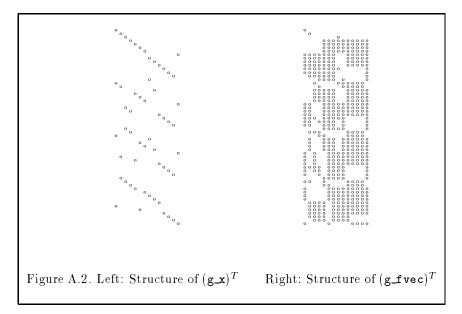


Figure A.1. Structure of the swirling flow Jacobian, n = 56

The derivative subroutine produced by ADIFOR is

```
subroutine g_dswrl3 (g_p_, nxmax, x, g_x, ldg_x,
$ fvec, g_fvec, ldg_x,
$ fjac, ldfjac, 1, eps, nint)
```

If we initialize g_x to a 56×56 identity matrix, and let $g_p=56$, and if ldg_x is at least 56, then on exit from g_dswr13 , g_fvec will contain the transpose of $\frac{\partial F}{\partial x}$, stored as a dense matrix. As it turns out, less than 7 % of the total operations performed with gradient objects in the ADIFOR code involve nonzeros. On the other hand, by using a graph-coloring algorithm designed to identify structurally orthogonal columns (we used the one described in [12]), we can determine that this Jacobian can be grouped into 14 sets of structurally orthogonal columns, independent of the size of the problem. In our example, columns 1, 16, 31, and 51 were in the first group; columns 2, 17, 37, and 43 were in the second group; and so on. We can take advantage of this fact by initializing the first column of g_x^T such that it has 1.0 in rows 1, 16, 31, and 51; by initializing the second column of g_x^T such that it has 1.0 in rows 2, 17, 37, and 43; and so on. The structure of g_x^T thus initialized is shown in Figure A.2 together with the resulting compressed Jacobian g_fvec^T . Note that instead of $g_p=56$ we now can get by with $g_p=14$, a sizable reduction in cost.



Assuming that color(i) is the "color" of column *i* of the Jacobian and that nocolors is the number of colors (in our example we had 14 colors), the following code fragment properly initializes g_x , calls g_dswr13 to compute the compressed Jacobian, and then extracts the Jacobian.

```
n = 14*nint
do i = 1, n
do j = 1, nocolors
g_x(j,i) = 0
enddo
g_x(color(i),i) = 1
enddo
call g_dswrl3 (nocolors, nxmax, x, g_x, pmax,
+ fvec, g_fvec, pmax,
+ fjac, ldfjac, 1, eps, nint)
c job = 1 indicates that only the function value is to be computed in
c dswrl3.
```

```
Revision D ADIFOR 2.0 User's Guide February 16, 1998
c nonzero(j,i) is TRUE if the (j,i) entry in the Jacobian is nonzero,
c and FALSE otherwise.
do i = 1, n
    do j = 1, n
        if (nonzero(j,i)) then
            jac(j,i) = g_fvec(color(i),j)
        else
            jac(j,i) = 0.0
        endif
        enddo
```

Experimental results using this approach on a suite of problems from the MINPACK test set collection are presented in [4, 10].

enddo

A.5 Case 4: Sparse Jacobian, two independent variables, one dependent variable

The coating thickness problem, conveyed to us by Janet Rogers of the National Institute of Standards and Technology, presents many alternatives for using ADIFOR-generated subroutines. The code for this problem is (in abbreviated form) shown below:

```
SUBROUTINE fun(n,m,np,nq,
     +
                     beta, xplusd, ldxpd,
     +
                     f.ldf)
c Subroutine Arguments
                   number of observations
с
      ==> n
       ==> m
                    number of columns in independent variable
С
       ==> np
                   number of parameters
с
      ==> na
                   number of responses per observation
с
      ==> beta
                   current values of parameters
с
      ==> xplusd current value of independent variable, i.e., x + delta
С
                   leading dimension of xplusd
       ==> ldxpd
С
      <== f
                   predicted function values
с
       ==> ldf
                    leading dimension of f
с
c Variable Declarations
      INTEGER
                       i, j, k, ldf, ldxpd, m, n, np, nq, numpars
      INTEGER
                       ia, ib
      DOUBLE PRECISION beta(np), f(ldf,nq), xplusd(ldxpd,m)
      double precision par(20), fn(2)
      do 10 k=1,np
        par(k) = beta(k)
   10 continue
      do 100 i=1,n
         do 20 j=1,m
           par(np+j) = xplusd(i,j)
   20
         continue
```

```
compute function values (fn) given parameters (par)
С
         call fnc(par,fn)
         f(i,1) = fn(1)
         f(i,2) = fn(2)
  100 continue
      return
      end
      subroutine fnc(x,fn)
      integer m,np,nq
      parameter (np=8,m=2,nq=2)
      integer i
      double precision x(np+m),fn(nq)
      double precision beta(np),xplusd(m)
      do 10 i=1,np
        beta(i) = x(i)
   10 continue
      do 20 i=1,m
         xplusd(i) = x(np+i)
   20 continue
c compute first of multi-response observations
   fn(1) =
           beta(1)
    +
                          + beta(2)*xplusd(1)
     +
                          + beta(3)*xplusd(2)
     +
                          + beta(4)*xplusd(1)*xplusd(2)
c compute second of multi-response observations
   fn(2) =
            beta(5)
                          + beta(6)*xplusd(1)
     +
     +
                          + beta(7)*xplusd(2)
                          + beta(8)*xplusd(1)*xplusd(2)
     +
      return
      end
```

The special format of this code is due to its embedding in the ODRPACK software for orthogonal distance regression. We are interested in the derivatives of f with respect to the variables **beta** and **xplusd**. We shall explore various ways to do this in some detail.

A.5.1 Approach 1 – Generate derivatives only for fnc

The easiest approach is to generate the derivative code only for fnc, since it is clear from the code that f(i,1:2) depends only on beta(1:np) and xplusd(i,1:m). ADIFOR then produces

subroutine g_fnc(g_p_, x, g_x, ldg_x, fn, g_fn, ldg_fn)
integer m, np, nq
parameter(np = 8, m = 2, nq = 2)

double precision x(np+m), fn(nq), g_x(ldg_x,np+m), g_fn(ldg_fn,nq)

If inside fun we replace the call to fnc with a call to g_fnc, always initializing g_x to a 10×10 identity matrix before the call, then

$$g_fn(k, j) = \frac{\partial f(i, j)}{\partial beta(k)}, k = 1, \dots 8, j = 1, 2.$$

 and

$$g_{fn}(\mathbf{k}, \mathbf{j}) = \frac{\partial f(\mathbf{i}, \mathbf{j})}{\partial \operatorname{xplusd}(\mathbf{i}, \mathbf{k} - \mathbf{np})}, k = 9, 10.$$

Closer inspection reveals that the 10×2 array g_fn always has the following structure (numbers are used to uniquely identify nonzero elements):

$$\left(\begin{array}{cccc} 1 & 0 \\ 2 & 0 \\ 3 & 0 \\ 4 & 0 \\ 0 & 5 \\ 0 & 6 \\ 0 & 7 \\ 0 & 8 \\ 9 & 10 \\ 11 & 12 \end{array}\right).$$

In other words, fn(i,1) depends only on beta(1:4), and fn(i,2) depends only on beta(5:8). Hence, we can compute a compressed version of g_fn at reduced cost by merging rows 1 and 5, 2 and 6, 3 and 7, and 5 and 8 of g_fn. Keeping in mind that g_fn is the *transpose* of the Jacobian, this is an especially simple case of the compression strategy outlined in the preceding section. This is achieved by initializing

which results in

$$\mathbf{g_fn} = \begin{pmatrix} 1 & 5\\ 2 & 6\\ 3 & 7\\ 4 & 8\\ 9 & 10\\ 11 & 12 \end{pmatrix}$$

All the nonzero values of the Jacobian are now computed at roughly 60% of the cost of the previous approach.

On a SPARC-compatible Solbourne 5E/900 with a clock resolution of 0.01 seconds, executing fun took 0.01 seconds, computing derivative values using g_fnc without compression took 0.06 seconds, and exploiting the structure of g_fn through the initialization of g_x shown above reduced that time to 0.03 seconds.

A.5.2 Approach 2 – Generate derivatives for fun

An alternative method of applying ADIFOR is to process subroutine fun. ADIFOR detects the interprocedural data dependence between fun and fnc and therefore generates g_fun as well as g_fnc, with g_fnc called properly within g_fun. We obtain

Now we have three-dimensional derivative objects, which somewhat complicates the initialization of g_xplusd and the interpretation of the results in g_f . However, this is not too difficult if we keep in mind that we wish to initialize

$$\begin{pmatrix} g_beta^T \\ g_xplusd^T \end{pmatrix}$$

to an identity matrix. The number of elements in **xplusd** is n*m, and the number of elements in **beta** is **np**. For the coating thickness problem, **n=63**, **m=2**, and **np=8**. Hence, the identity matrix should be 134×134 . This is also the value we shall use for **g_p_**. Initialization of **g_beta** follows the scheme outlined in Section A.3; that is, the first 8 rows should be an 8×8 identity matrix, and the remaining 126 rows should be initialized to zero. How to initialize **g_xplusd** is less readily apparent, for it is not immediately obvious how to form a 126×126 identity matrix from a three-dimensional structure. However, if one looks at the way Fortran stores two-dimensional structures in memory, a simple scheme for storing the Jacobian develops. In Fortran, element (j, i) in an $n \times m$ array is stored as if it were element n * (i - 1) + j of a one-dimensional array. Thus, we can apply this technique to map the 126 columns of the Jacobian that should be initialized to the identity onto **g_xplusd**. Specifically, element (np+k, j, i) is initialized to 1 if and only if k = 63 * (i - 1) + j. The following code segment accomplishes this initialization.

```
c n=63, m=2, np=8
```

```
g_p = np + m*n
    do 44 i = 1, np
     do 144 j = 1, g_p
        g_{beta}(j,i) = 0.0
144
     continue
     g_{beta}(i,i) = 1.0
44 continue
   do 45 i = 1, m
     do 145 j = 1, n
        do 245 k = 1, g_p_
          g_xplusd(k,j,i) = 0.0
245
        continue
        g_xplusd(np+((i-1)*n)+j,j,i) = 1.0
145
     continue
 45 continue
```

When initialized in this manner, ADIFOR computes

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$$\mathbf{g}_{-}\mathbf{f} = \left(J_f = \left(\frac{\partial f}{\partial beta}, \frac{\partial f}{\partial xplusd}\right)\right)^T.$$

However, the performance of this approach is poor, since we totally ignore the sparsity structure of the Jacobian. As a result, the computation of J_f takes 0.77 seconds on a Solbourne 5E/900. A better way to find the Jacobian of **f** using **g_fun** is to take note of the structures used by **fun**. From this, it becomes obvious that $\frac{\partial f[i,j]}{\partial xplus d[k,l]}$ is nonzero only when i = k. As a consequence, we may change the

```
g_p = np + m*n
. . .
g_xplusd(np+((i-1)*n)+j,j,i) = 1.0
```

to the much simpler

```
g_p = np + m
. . .
g_xplusd(np+i,j,i) = 1.0
```

with the understanding that $g_f(np+i,j,k)$ (i = 1..m) represents $\frac{\partial f[j,k]}{\partial x plus d[j,i]}$. This is equivalent to initializing

This implementation is much more efficient than that described in the preceding paragraph and more closely mimics the behavior of the original subroutine fun. As a consequence, the time required to execute g_fun using this initialization is 0.07 seconds.

As discussed in Section A.5.1, only half of the derivatives of **f** with respect to **beta** are nonzero. Specifically, $\frac{\partial f[i,1]}{\partial beta[j]}$ is nonzero for j = 1..4 and zero for j = 5..8, while $\frac{\partial f[i,2]}{\partial beta[j]}$ is zero for j = 1..4 and nonzero for j = 5..8. This information can be used to further compress the Jacobian. The initialization

compresses the Jacobian into only 6 columns. Columns 1 through 4 represent the nonzero derivatives of **f** with respect to **beta**, while columns 5 and 6 correspond to the derivatives of **f**[i,j] with respect to **xplusd**[i,1..2], as above. This initialization may be accomplished with the following code fragment.

```
c n=63, m=2, np=8
     halfnp = 4
      g_p = 4 + m
      do 44 i = 1, halfnp
       do 144 j = 1, g_p_
          g_beta(j,i) = 0.0
          g_beta(j,i+halfnp) = 0.0
 144
       continue
       g_{beta}(i,i) = 1.0
       g_beta(i,i+halfnp) = 1.0
  44 continue
      do 45 i = 1, m
       do 145 j = 1, n
          do 245 k = 1, g_p_
           g_xplusd(k,j,i) = 0.0
 245
          continue
          g_xplusd(halfnp+i,j,i) = 1.0
       continue
 145
  45 continue
```

This approach is efficient, capable of computing all derivatives in 0.03 seconds. However, it has the disadvantage that the initialization routine might have to be changed if **fnc** or **np** is altered.

A.6 Computing Gradients of Partially Separable Functions

A particular class of functions that arises often in optimization contexts is that of the so-called partially separable functions [14, 19, 20, 21, 22]. That is, we have a function $f : \mathbf{R}^n \to \mathbf{R}$ that can be expressed as

$$f(x) = \sum_{i=1}^{nf} f_i(x).$$

Usually each f_i depends on only a few (say, n_i) of the x's, and one can take advantage of this fact in computing the (sparse) Hessian of f.

As was pointed out to us by Andreas Griewank, now at the University of Dresden, this structure can be used advantageously in computing the (usually dense) gradient ∇f of f.

Assume that the code for computation of f looks as follows:

```
subroutine f(n,x,fval)
integer n
real x(n), fval, temp
fval = 0
call f1(n,x,temp)
fval = fval + temp
```

```
call fnb(n,x,temp)
fval = fval + temp
return
end
```

If we submit f to ADIFOR, it generates

.

```
subroutine g_fn(g_p_,n,x,g_x,ldg_x,fval,g_fval,ldg_fval).
```

To compute ∇f , the first (and only) row of the Jacobian of f, we set $g_{-p_{-}} = n$ and initialize g_x to a $n \times n$ identity matrix. Hence, the cost of computing ∇f is of the order of n times the function evaluation.

As an alternative, we realize that with $f: \mathbf{R}^n \to \mathbf{R}^{nb}$ defined as

$$g = \left(\begin{array}{c} f_1\\ \vdots\\ f_{nb} \end{array}\right),$$

we have the identities

$$f(x) = e^T g(x)$$
, and hence $\nabla f(x) = e^T J_g$

where e is the vector of all ones, and J_g is the Jacobian of g. We can get the gradient of f by computing J_g and adding up its rows. The corresponding code fragment for computing f is

```
subroutine f(n,x,fval)
integer n
real x(n)
integer nf, i
parameter (nf = <whatever>)
real gval(nf)
call g(n,x,gval)
fval = 0
do i = 1,nb
   fval = fval + gval(i)
enddo
return
end
```

It may not appear that we have gained anything, since J_g is $nf \times n$. If we initialize g_x in

```
subroutine g_g(g_p_,n,x,g_x,ldg_x,gval,g_gval,ldg_gval)
```

to an $n \times n$ identity matrix, then the computation of J_g still takes about n times as long as the computation of g (or f).

The key observation is that the Jacobian J_g is likely to be sparse, since

$$J_g = \begin{pmatrix} (\nabla f_1)^T \\ \vdots \\ (\nabla f_{nb})^T \end{pmatrix},$$

and each of the f_i 's depends only on n_i of the x's. By using the graph coloring techniques described in Section A.4, we can compute J_g at a cost that is proportional to the number of columns in the compressed J_g , and then add up its (sparse) rows. As a result, we can compute ∇f at a cost that is potentially much less than n times the evaluation of f. Alternatively, we can employ the SparsLinC library (see Appendix C), which will exploit sparsity even if the Jacobian contains a few dense rows (in this case, its chromatic number is n, and nothing has been gained). Experimental results with partially separable functions from the MINPACK test set collection are presented in [5].

Appendix B

ADIntrinsics 1.5: Exception Handling Support for ADIFOR 2.0

B.1 Introduction

In ADIFOR parlance, an "exception" is an event that occurs when an elementary function is evaluated at a point where the function result is defined, but the derivative is not. For instance, the square root of zero is zero, but the derivative of the square root function at zero is not defined. For most functions, there are several reasonable interpretations of what should be done when an exception occurs.

ADIFOR 2.0, by default, chooses the approach that was deemed appropriate for most cases, based on the arguments presented in [8, 23]. However, only a person familiar with the code can decide whether this choice is the correct one for a particular given instance. Hence, when an exception occurs, one should examine the derivative code generated by ADIFOR 2.0 to make sure that the default values had the desired effect. Section B.2 describes **what every user should do to be aware of the occurrence of such exceptions**. Section B.3 defines exceptional occurrences in ADIFOR 2.0 and the default action taken.

In dealing with FORTRAN 77 intrinsics, the ADIFOR 2.0 system relies on the ADIntrinsics system which has been developed mainly so that a user can easily customize the behavior of ADIFOR in the cases where the default option turns out to be inappropriate. It allows the user to specify alternative strategies through directives in the code to be differentiated and alternate template files, thereby documenting the changes and obviating the need to manually post-process the ADIFOR-generated code. The ADIntrinsics system also allows one to switch between different error reporting flavors. To achieve this flexibility, derivative code generation in ADIFOR 2.0 is split into two phases:

- 1. ADIFOR 2.0 generates code containing invocations of "templates" at call sites of FORTRAN 77 intrinsics. This code is contained in the files with the .A suffix in the AD_DUTPUT_DIR directory.
- 2. The purse postprocessor expands the templates into explicit Fortran code.

These two steps are usually transparent to users as these two components are invoked directly by the Adifor2.0 command. Section B.4 describes the different exception handler modes in details.

To link ADIntrinsics into your executable, you must add one of the following to your link line:

... \$AD_LIB/lib/ReqADIntrinsics-\$AD_OS.o \
 -L \$AD_LIB -lADIntrinsics-\$AD_OS # in UNIX

 \mathbf{or}

```
... $AD_LIB/lib/ReqADIntrinsics-$AD_OS.o \
    $AD_LIB/lib/libADIntrinsics-$AD_OS.a # in UNIX
```

 \mathbf{or}

The reason for not combining the two files in one archive is that the .o file contains some block data initializations which may not get linked into your executable if they are contained in the archive. In section B.5, we describe how to change the exception reporting options, such as, for example,

- 1. changing the exception handler output unit,
- 2. resetting the exception handler counts,
- 3. dynamically changing between different levels of exception reporting, or
- 4. ignoring exceptions in particular regions of code.
- 5. Section B.6 describes how to redefine the exceptional values returned at points of nondifferentiability, either by changing globally the definitions of default values for certain exception classes, or by changing the behavior associated with a particular intrinsic.

Lastly, in Section B.7, we present an example of employing some of these features. We also mention that the user can go beyond what is described here in redefining the behavior of the exception handler by redefining the templates governing the purse translation. These issues will be described in a forthcoming edition of this user guide.

B.2 What Every User Should Do

To obtain a summary report on intrinsic exceptions, one should *always* call the routine **ehrpt** (for exception handler report) after the call to the ADIFOR-generated procedure derived from the top-level subroutine.

```
program main
[...]
call ADIFOR_GENERATED_CODE ()
[...]
call EHRPT
return
end
```

B.3 Definition of Intrinsic Exceptions and Default Behavior

Some of the FORTRAN 77 intrinsics are not globally differentiable at all points of their domain, such as, for example, $\frac{d\sqrt{x}}{dx}|_{x=0}$. However, the propagation mechanism employed in automatic differentiation requires that *some value* be returned for that derivative. Table B.1 lists the five types of exceptional values employed, their default value (in brackets), and their interpretation.

Exceptional Value [Default]	Interpretation
JumpVal[0]	The function is discontinuous at this point.
NoLimit[0]	The directional derivatives do not agree.
TieVal[0.5]	The case $x = y$ for min and max.
InfVal[0]	The derivative approaches infinity.
NaNVal[0]	Not even a generalized interpretation makes sense.

Intrinsic	f_x undefined	Default Value
AINT(x)	$x = \pm 1, \pm 2, \dots$	JumpVal
ANINT(x) and DNINT	x = odd multiples of 1/2	JumpVal
ABS(x)	x = 0	NoLimit
MOD(x,y)	x = n * y for an integer n	JumpVal
SIGN(x,y)	x = 0 or $y = 0$	JumpVal
DIM(x,y)	x = y	NoLimit
MAX(x,y)	x = y	TieVal
MIN(x,y)	x = y	TieVal
SQRT(x) real-valued x	x = 0	InfVal
SQRT(x) complex-valued x	x = 0	NaNVal
ASIN	$ x \geq 1$	InfVal
ACOS	x > 1	InfVal

Table B.1. Exceptional Derivative Values

Table B.2. Points of Nondifferentiability and Default Values of Partial for unary FORTRAN 77 Intrinsics

These default exceptional values are employed as shown in Tables B.2 and B.3. We employ the shorthand f_x and f_y to denote the partial derivative with respect to the first and second argument, respectively.

In case of a complex-valued argument, abs(x) is treated like sqrt(re(x)**2 + im(x)**2), and hence has the same exceptional behavior like the real-valued square root.

The following principles were considered in designing the ADIFOR exception-handling mechanism (see [8, 23] for more background information):

- **Generalized Gradient:** Many algorithms for optimizing nonsmooth functions use generalized gradient values. A generalized gradient is any value in the convex hull of derivative values in the neighborhood of the point of nondifferentiability. For univariant functions, one may obtain any value in the interval $[\liminf f', \limsup f']$. For example, a generalized gradient for |x| at 0 is any number in [-1, 1]. The values we choose to return as "derivative" values at points of nondifferentiability are generalized gradient values, provided that the chain rule for generalized gradients holds as a set inequality, rather than as an inclusion [11].
- **Continuity of Catastrophe:** The value at the point of nondifferentiability should in some sense be the limit of what happens in a neighborhood. For example, the derivative of asin (x) at 1 should be **INFINITY**. For some functions, the mathematical limit may be different from the computational limit, as a result of finite precision or denormalized numbers.

Extreme Point: A necessary condition for the existence of an extreme point is f' = 0. A point of

Intrinsic	f_x undefined	Default for f_x	f_y undefined	Default for f_y
MOD(x,y)	x = n * y for an integer n	JumpVal	never	N/A
$\operatorname{SIGN}(x,y)$	x = 0 or $y = 0$	JumpVal	never	N/A
DIM(x,y)	x = y	NoLimit	x = y	same as for f_x
MAX(x,y)	x = y	TieVal	x = y	$f_y = 1 - f_x$
MIN(x,y)	x = y	TieVal	x = y	$f_y = 1 - f_x$
x * * y	x = 0 and 0 < y < 1	InfVal	x < 0 or $(x = 0 and y = 0)$	NoLimit

Table B.3. Points of Nondifferentiability and Default Values of Partials of binary FORTRAN 77 Intrinsics

nondifferentiability is usually at least a local extreme point, so returning a value of 0 as the derivative may signal an optimization algorithm that an extreme point has been found.

- **Evaluation of Undefined Functions:** In some computing environments, execution may continue after an attempt to evaluate a function at a point outside its domain (perhaps with a value of NaN). If the program has not crashed while evaluating $\sqrt{-2.0}$ (in real arithmetic), then our derivative evaluation should not crash, either.
- Scaling: It is critical to scale many applications appropriately before applying an optimization or ODE-solving algorithm. In many calculations, variable vectors are scaled by their L_1 norm or L_{∞} norm (i.e., the sum or maximum of the component moduli). Later on, this scaling is undone so that the overall calculation is mathematically smooth, even when some of the components are zero or their absolute values are tied at the maximum. The derivative is locally not defined, but the entire computation is globally differentiable. We have attempted to return derivative values that make sense in connection with commonly used scaling techniques.

These principles often conflict with one another and have different implications regarding the values that should be returned at points of nondifferentiability. We made trade-off choices that we think can be justified.

For sqrt, at the point of nondifferentiability x = 0, the default for InfVal = 0 is a generalized gradient value if we assume that sqrt(x) := sqrt(abs(x)). Further, it makes expressions like $sqrt(X^*X^*X + Y^*Y^*Y)$ have the correct derivative. However, it violates the principle of continuity of catastrophe. Alternatively, the value of InfVal = INFINITY makes the one-sided limit correct. For asin and acos, at the points of nondifferentiability $x = \pm 1$, the default for InfVal= 0 indicates an extreme point. However, it violates the principle of continuity of catastrophe. Alternatively, the value of InfVal = INFINITY makes the one-sided limit correct. If |x| > 1, usually the user's original code will have already crashed while evaluating asin(x). If it has continued execution (perhaps with value NaN), we should continue execution also. No value is reasonable since the function is not defined, so we choose to return the same value as at $x = \pm 1$. Alternatively, we could return whatever was assigned to the value of asin(x).

For the sign function, at the point of nondifferentiability x = 0, the default value of 0 for NoLimit is a generalized gradient value equal to the average of the two limits from each side. Using NoLimit = 0 also provides a generalized gradient for abs at the point of nondifferentiability x = 0and indicates an extreme point. This choice also satisfies the generalized gradient requirement for dim at the points of discontinuity, x = y.

The derivatives of **aint** and **anint** are set to **JumpVal** at the points of nondifferentiability, and 0 elsewhere. The default value for **JumpVal** is 0, the limit from each side. The derivative of **mod** is also set equal to **JumpVal** at points of discontinuity. Although the default value of 0 is not equal to

the limit from both sides, which is 1, it does signal an extreme value, important for optimization.

The default value for TieVal is 1/2. This value has the benefit that it is a generalized gradient and implies that if x = y then $f_x = f_y$. However, Fortran's max and min functions accept more than two arguments. Consequently, the current implementation of ADIFOR breaks all calls to min and max into a series of binary calls. Thus, if many arguments are equal, their slopes are weighted 1/2, 1/4, 1/8,

B.4 Exception Handler Modes

The exception handler operates in five modes: verbose, report-once, counting, terse, and performance. The default mode is **reportonce**. Note, however, since **reportonce** requires the compilation of some C libraries, if your system does not support a C compiler, you will need to override this default by setting AD_EXCEPTION_FLAVOR to one of performance, terse, counting, or verbose.

In verbose mode, *every time* an exceptional condition occurs, a message is written to the program's error unit (by default unit number zero, which usually outputs to the screen) indicating the function, the arguments to the function, and the file name and line number containing this function evaluation. A sample output line is shown in Figure B.1. This information allows one to track down

Figure B.1. Verbose Mode Sample Error Report

exactly where the exception is occurring and decide whether it is generating appropriate results. However, this option may generate a significant amount of output.

Report-once mode combines all of the exception reports for a source line into a single report, as shown in Figure B.2.

In addition, counting, terse, and performance modes provide a decreasing amount of information about exceptions that occur.

Note: Unless you invoke the exception handler reporting routine ehrpt after the execution of the ADIFOR-generated code, you will not see any of the reports generated by the report-once, counting, and terse modes.

Counting mode maintains a running total of each *type* of exception that occurs, as shown in Figure B.3. It avoids the work associated with tabulating exceptions in report-once mode, and hence should execute faster.

Terse mode indicates whether any exceptions of a given type occurred. This mode may be useful for vectorizing compilers, where the recurrence required for counting may inhibit vectorization. A sample terse mode output is given in Figure B.4.

Performance mode contains only a minimal amount of exception-checking code. It makes no subroutine calls and always assigns the default value when an exception occurs. We suggest that one should only use performance mode after running the code with report-once or verbose mode and convincing oneself that either no exceptions occur or the default exception handling is appropriate. The following sections describe how to change the default handling in case it is not. No report is made, since no exceptions are tracked.

```
At line 100 in file "g_func.f", while executing routine "foo",
an exception occurred evaluating ABS : 50 times.
```

At line 3 in file "g_misc.f", while executing routine "bar", an exception occurred evaluating ABS : 1 time.

At line 7 in file "g_misc.f", while executing routine "bar", an exception occurred evaluating POWER: df/dx : 5 times.

At line 17 in file "g_misc.f", while executing routine "bar", an exception occurred evaluating ACOS first deriv : 17 times.

At line 920 in file "g_misc.f", while executing routine "bar", an exception occurred evaluating ABS : 49 times.

Figure B.2. Report-once Mode Error Report

Double precision exception(s) occurred evaluating		
ABS	:	100 times.
POWER: df/dx	:	5 times.
ACOS first deriv	:	17 times.

Figure B.3. Counting Mode Error Report

Double precision exception(s) occurred evaluating: ABS POWER ACOS first deriv



The exception handling mode may be chosen at the time ADIFOR 2.0 is executed by setting the AD_EXCEPTION_FLAVOR variable to one of: performance, terse, counting, reportonce, or verbose.

B.5 Changing Exception Reporting Options

B.5.1 Redirecting Exception Handler Output

Two different routines are provided for report-once mode and the remaining exception handling modes. Two different routines are necessary as report-once mode is generated by a C subroutine, whereas all other output modes are generated by Fortran code.

Report-once Mode — **ehofil:** To direct the output of report-once mode to a file, call **ehofil** with the name of the output file, e.g.,

```
call ehofil ('reportonce.out')
```

All Modes but report-once — ehsup: To direct the exception handler output for all modes but report-once to a different unit, open the unit in your driver program, and then call ehsup with two parameters: -1, and then the unit number. The driver is also responsible for closing this unit before the program terminates. Failure to do so may result in a loss of output that has been buffered but not written to the file.

call ehsup (-1, UNIT-NUMBER)

A segment of the user code might resemble this fragment.

```
open (UNIT=13, FILE='adifor-errors.out')
call ehsup (-1, 13)
[... Useful Work ...]
close(13)
```

B.5.2 Resetting Exception Counts

The routine ehrst causes all counts of exceptions to be reset to zero. An example of use is

call ehrst()

B.5.3 Fine-Grained Control of Exception Handler Modes

Fine-grained control over exception handler modes is achieved by embedding directives in the user's code.

Change of Verbosity Level: The verbosity level can be dynamically set with the AD_EXCEPTION_LEVEL() directive. Valid levels are verbose, counting, terse, reportonce, performance, and default, which restores the exception level to the one with which ADIFOR 2.0 was run. For example, to guarantee verbose exception reporting around a certain region, the user might use the following code:

Revision \mathbf{D}

```
C AD_EXCEPTION_LEVEL(VERBOSE)
[... Interesting Code Here ...]
C AD_EXCEPTION_LEVEL(DEFAULT)
```

Warning:

Terse mode is incompatible with both counting mode and verbose mode in the sense that switching from verbose or counting mode to terse mode anywhere in your program leads to incorrect summary information being reported by **ehrpt**.

If you intend to use the report-once mode anywhere in your program, you must run ADIFOR 2.0 with the AD_EXCEPTION_FLAVOR=reportonce binding. Otherwise, report-once mode will not function properly.

Ignoring Exceptions in a Region: To ignore exceptions in a region, bracket the region with the directives AD_EXCEPTION_BEGIN_IGNORE and AD_EXCEPTION_END_IGNORE. "Ignoring" exceptions simply means that no exceptional information is printed out; it does not mean that the exception handler is disabled.¹ Truly disabling the exception handler (that is, using performance mode) should be done with caution, because at exceptional points the performance mode may return a value different than that returned by the exception handler for a user-configured value.

C AD_EXCEPTION_BEGIN_IGNORE() [... Exceptions to be Ignored Here ...] C AD_EXCEPTION_END_IGNORE()

Warning: These directives do not nest. This means that any AD_EXCEPTION_END_IGNORE cancels all previous AD_EXCEPTION_BEGIN_IGNORE commands, regardless of how many preceded the end ignore.

Here is an example showing how the ignore directives do not nest.

С	AD_EXCEPTION_BEGIN_IGNORE()
	[Exceptions are Ignored Here]
С	AD_EXCEPTION_BEGIN_IGNORE()
	[Exceptions are Ignored Here]
С	AD_EXCEPTION_END_IGNORE()
	[Exceptions are REPORTED Here]
С	AD_EXCEPTION_END_IGNORE()
	[Exceptions Continue to be Reported Here]

Syntax of Directives: The syntax of the directives is intended to be reasonably intuitive:

- any comment character (C, c, or *) may be used to begin the comment line;
- spaces cannot appear in the middle of a keyword, but may appear around parentheses and commas;
- the directives can appear in upper or lower case, as can the keywords (arguments) given; and

 $^{^{1}}$ Currently, the "ignore" mode is implemented by placing the exception handler in counting mode for the given region.

• zero or more whitespace characters may appear between the comment character and the beginning of the directive, but no other spurious characters should appear in the line, even after column 72.

Warning: Directives affect only the parts of the program that are *literally* after them. In particular, a directive cannot change the mode in which an invoked procedure runs. The example below shows *incorrect* usage of the AD_EXCEPTION_LEVEL directive.

```
C This is an incorrect use of the AD_EXCEPTION_LEVEL directive.
C it has no effect on the subroutine "slow_func".
C AD_EXCEPTION_LEVEL(PERFORMANCE)
        call slow_func
C AD_EXCEPTION_LEVEL(DEFAULT)
```

B.6 Modifying Exceptional Behavior

For each of the FORTRAN 77 intrinsics that are not globally differentiable, **purse** requires a default value to be inserted for the first (and sometimes also second) partial derivatives at the point of nondifferentiability.

It is possible to override the default behavior for the exceptions. This overriding is precisionspecific, and is done through the routines **ehsev*** and **ehsup***, where ***** is one of **s**, **d**, **c**, or **z**, for single, double precision, complex, or double complex, respectively. The first one changes the values associated with the symbolic exception values **InfVal**, etc. (see section B.3), the second changes the exceptional behavior associated with a particular intrinsic function.

B.6.1 Changing Exception Class Default Values

The routines ehsev*, where * is one of s, d, c, or z, for single, double precision, complex, or double complex, respectively, allow the user to set the symbolic exceptional values "InfVal", "NaNval", "NoLimit", "TieVal", and "JumpVal".

The usage is

```
call ehsev* (SYMBOLIC-NUMBER, NEW-VALUE)
```

where SYMBOLIC-NUMBER is the integer number of the symbolic exceptional value from Table B.4, and NEW-VALUE is the floating point numerical value to set. So for example, to set TieVal to zero

Symbolic Name	Number
InfVal	1
NaNval	2
NoLimit	3
TieVal	4
JumpVal	5

Table B.4. Numbering of Symbolic Exceptional Values

for double precision, one would execute

call ehsevd(4,0.0d0)

It is important that the numerical value be of the right type, as there is, in general, no guarantee that the compiler would convert it to the right type.

B.6.2 Changing Exceptional Behavior for a Particular Intrinsics

To override the exceptional behavior of a particular intrinsic, one needs to know two facts: the integer that represents the intrinsic for which the exception is occurring, and the integer "offset" of the exceptional condition whose return value is to be altered. The integer representing the intrinsic can be found in Table B.5.

Intrinsic	Numerical Value
AINT	1
ANINT	2
DNINT	2
ABS	3
MOD	4
SIGN	5
DIM	6
MAX	7
MIN	8
SQRT	9
currently not used	10
currently not used	11
**	12
ASIN	13
ACOS	14
SQRT4CABS	15

Table B.5. Numbering of Intrinsic Functions

Note: The SQRT4CABS "function" is a dummy intrinsic generated by ADIFOR 2.0 to handle the complex ABS function. Let z = x + iy. The complex ABS(z) function is rewritten as

$$abs(z) = SQRT4CABS(x^2 + y^2)$$

By default, SQRT4CABS has the same exceptional behavior as SQRT.

Single Exceptional Condition

All intrinsics except for the power operator ** have only a single exceptional condition (see Tables B.2 and B.3) and therefore have an offset of one. Suppose one wishes to change the exceptional value of **ABS** at zero (for both real and double precision) so that the partial derivative of **ABS**(**x**) with respect to **x** at zero is one. First, one would look in Table B.5 to find that the integer representing **ABS** is 3. Hence, one would use the following two calls to set the desired partials of **ABS**.

```
C Set single precision partial of abs
call ehsups (3,1,1.0e0)
```

```
xabs = abs(x)
yabs = abs(y)
w = max(xabs,yabs)
if (w .eq. 0.0) then
    z = 0.0
else
    z = w*sqrt( (xabs/w)**2 + (yabs/w)**2 )
endif
```



C Set double precision partial of abs call ehsupd (3,1,1.0d0)

Handling of the POWER operator (**):

As indicated in Table B.5, the integer representing the power operator is 12. The partial with respect to x is associated with an offset of 1, the partial with respect to y is associated with an offset of 2, for example:

```
C Set single precision partial w.r.t. x of **
    call ehsups (12,1,1.0e0)
C Set double precision partial w.r.t. y of **
    call ehsupd (12,2,1.0d0)
```

B.7 Examples of the Use of ADIntrinsics

As an example, consider the computation of the Euclidean norm $z = \sqrt{x^2 + y^2}$. A numerically sensible way of doing this is shown in Figure B.7. This function is differentiable except for x = y = 0. However, automatically differentiating with respect to **x** and **y**, we note that we might attempt to compute the derivatives of **abs()** when its argument is zero, and of **max()** when both its arguments have the same value, even when x and y are not both zero. By default, the ADIntrinsics system would invoke the error handler, which would report these exceptions to the user. However, we know that, unless x = y = 0, this computation represents a differentiable function and that, independent of the value of **w**, we will obtain the same result.

Thus, as shown in Figure B.7, we go into "performance mode" in the part of the code that generates exceptions that are merely caused by our use of scaling, thus avoiding invocation of the error handler altogether. Also, since the value w did not have an impact on the computed value, the value for the derivative of w will not matter, either. For x = y = 0, we trigger an invocation of the ADintrinsics error handler at the point of nondifferentiability by replacing z = 0 with $z = \operatorname{sqrt}(w)$. When translated by ADIFOR, the generated derivative code will report a "SQRT" exception only at x = y = 0.

```
С
      AD_EXCEPTION_LEVEL(PERFORMANCE)
      xabs = abs(x)
      yabs = abs(y)
      w = max(xabs,yabs)
С
      AD_EXCEPTION_LEVEL(DEFAULT)
      if (w .eq. 0.0) then
С
      the sqrt(0.0) call triggers exception reporting
         z = sqrt(w)
      else
      AD_EXCEPTION_LEVEL(PERFORMANCE)
С
         z = w*sqrt((xabs/w)**2 + (yabs/w)**2)
С
      AD_EXCEPTION_LEVEL(DEFAULT)
      endif
```

Figure B.6. Computation of Euclidean Norm Annotated for Subsequent Automatic Differentiation

Appendix C

Sparse Derivative Support for ADIFOR 2.0 through the SparsLinC 1.1 Library

C.1 Introduction

SparsLinC 1.1 (**Sparse Linear Combinations**) is a library of C routines that provide an implementation of the "vector linear combination":

$$w = \sum_{i=1}^{k} \alpha_i * v_i, \tag{C.1}$$

employing sparse data structures. Here w and the v_i are vectors, the α_i are scalar multipliers, and k is referred to as the arity. This operation is the fundamental computational kernel for first-order automatic differentiation.

To link SparsLinC into your executable, you must add one of the following to your link line:

... -L\$AD_LIB/lib -lSparsLinC-\$AD_OS # in UNIX

 \mathbf{or}

... \$AD_LIB/lib/libSparsLinC-\$AD_OS.a # in UNIX

or

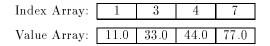
... %AD_LIB%\lib\libSparsLinC.lib # in Windows~95/NT

SparsLinC utilizes dynamic data structures to represent only the nonzero information contained in each vector and performs the vector linear combinations on these sparse representations of the vectors. By doing so, it avoids storing zero values and performing computation with zeros, at the cost of introducing some overhead associated with maintaining sparse data structures.

One way of representing a sparse vector with nnz nonzeros in Fortran is by means of two arrays, each of length nnz, one an integer array containing the indices of the nonzero entries, and the other

a floating-point array of appropriate precision, containing the corresponding values. So, for example, the 7-vector

would be represented by



We will refer to this 2-array representation of the vector as the **Fortran Sparse Format**. The corresponding nonsparse representation, which we will call the **Fortran Nonsparse Format**, would be a floating-point array of length 7, containing zeros in entries 2, 5, and 6. Lastly, there is the **SparsLinC Sparse Format**, which is the internal SparsLinC representation of the vector.

In addition to reducing the space required to store derivative values and the time required to compute derivatives, SparsLinC is also useful for uncovering the sparsity features of a problem. For example, the detection of the sparsity pattern of Jacobians is of interest in a number of computations. The computation of the Jacobian using SparsLinC yields the sparsity pattern of the Jacobian as a natural consequence of the work it does in computing the Jacobian, and thus provides all the information needed for a sparse equation solving routine, for example. We anticipate that this feature of SparsLinC will be further strengthened in future releases with the addition of diagnostic capabilities about the "sparsity behavior" of a computation.

From the user's point of view, using SparsLinC is very simple. Much of the task of interfacing ADIFOR 2.0-generated code and SparsLinC is done automatically and is transparent to the user. Section ?? describes how to invoke ADIFOR 2.0 to generate derivative code that uses the SparsLinC library. Such code will be referred to as "sparse derivative code." We will refer to derivative code generated by ADIFOR 2.0 in the default case (i.e., with do-loop implementation of vector linear combinations, rather than calls to SparsLinC routines) as "nonsparse derivative code."

Section C.2 provides some background information necessary to understand the use of SparsLinC with ADIFOR 2.0. Section C.3 defines the notion of sparsity and discusses computational scenarios where sparsity exists and can be exploited by SparsLinC for faster, less memory-intensive code. In the tutorial example given in Chapter 4, Step 4 describes, for the nonsparse (default) case, how to incorporate the ADIFOR 2.0-generated derivative code in the derivative code driver. Section C.4 outlines how this is done in the sparse derivative code driver by calling the appropriate **SparsLinC Access Routines**. These routines are the subset of SparsLinC routines that allow the user to set up and configure SparsLinC, pass data to it, and extract results and performance measures from it. Section C.5 describes how to build a sparse derivative code by using ADIFOR 2.0 and SparsLinC. Section C.6 contains detailed description of the SparsLinC access routines.

C.2 Background

In ADIFOR 2.0, an **active variable** is one that lies on a dependency path from the independent to the dependent variables (the independents and dependents themselves are also considered to be active). Active variables are the ones for which we compute **directional derivatives** with respect to a set of (not necessarily normalized) directions specified via the seed matrix. In the simplest case, each unit direction is defined by one of the independent variables, which is equivalent to setting the seed matrix to be the identity.

We define the term **directional gradient vector** to be the set of directional derivatives of any scalar active variable with respect to all directions specified in the seed matrix. The term **scalar active variable** here refers both to active variables declared as scalars in the user's Fortran source

code and to the individual elements of active variables that are declared as arrays. The directional gradient vectors appear as vector operands in the vector linear combinations equation (C.1).

C.3 Where Is SparsLinC Useful?

The main rationale for the development of SparsLinC is to make derivative computation run faster and use less memory. But not every problem will result in faster code if SparsLinC is used. The potential gain depends, to a large extent, on the inherent sparsity present in any particular derivative computation.

C.3.1 Definition of Sparsity

In a nonsparse representation, a directional gradient vector V would be declared as an array of length p, where p is the number of directions (i.e., the number of columns in the seed matrix).¹ We denote the number of nonzeros in V at a given point t during the execution by $V_{t.nnz}$. The percentage of zero entries or **sparsity** of V_t is defined as

$$V_{t.sparsity} := \left(1 - \frac{V_{t.nnz}}{p}\right) * 100\%.$$
 (C.2)

A good measure for the **overall sparsity** present in a derivative computation is the median of the sparsities of all directional gradient vectors *during the entire execution of the derivative code*.

A necessary (but not sufficient) condition for SparsLinC to improve the runtime performance of derivative computation is that the number of directions with respect to which we wish to compute derivatives be "large". This is perhaps an obvious, but nonetheless significant, point, since if the number of directions is small, directional gradient vectors will be short and any strategy to exploit sparsity will be defeated by the overhead associated with implementing that strategy. The determination of what is considered a large sparse problem is to a great extent dependent upon the nature of the problem; however, in our experience, the threshold at which our strategy becomes effective is 20–30 directions.

Another important issue concerning sparsity in derivative computations is that the sparsity of the final result (the nonzero structure of the final directional gradient vectors of the dependents) is only a lower bound on the sparsity of the intermediate directional gradient vectors; that is, the overall sparsity of the problem may be (and often is very) much higher than that of the final derivative result. In general, sparsity diminishes as the computation proceeds, because for all vector linear combinations, the nonzero index set of the resulting left-hand-side vector is the union of index sets of the right-hand-side vectors.² As a consequence, in many problems, there may be a lot of "hidden" sparsity that can be exploited by using SparsLinC.

C.3.2 Sparse Derivative Problem Types

The numerical computation of gradients and Jacobians is an important step in the solution of many nonlinear problems, such as constrained optimization, mesh computations, and the solution of systems of stiff differential and algebraic equations. In many instances, these problems require deriva-

¹For the sake of clarification, we note that p denotes the same quantity as the Fortran variable g_p_, used elsewhere in this document.

² This discussion precludes the possibility of the occurrence of numerical zeros resulting from exact cancellation (e.g., a + (-a)) and zero multipliers. In our experience, exact cancellation rarely occurs in derivative computation, and currently, SparsLinC does not check for it (i.e., numerically zero vector entries are treated like nonzero entries). SparsLinC does, however, check for zero multipliers, and vectors with zero multipliers are not referenced.

tive computations that have inherent sparsity. Two examples are gradients of partially separable functions and sparse Jacobians.

A function is partially separable if it can be represented as

$$f(x) = \sum_{i=1}^{m} f_i(x),$$
 (C.3)

where *m* is the number of partitions, and where each component function, $f_i(x)$, is typically a function of just a few of the elements of *x*, implying that each of the corresponding directional gradient vectors, $\nabla f_i(x)$, will be sparse, even though the aggregate *f* depends on all of *x*, leading to a dense final gradient $\nabla f(x)$. Any *f* with a sparse Hessian belongs to this class of problem [19], regardless of whether the partially separable structure is expressed explicitly in the code.

For many Jacobian computations, the final Jacobian is itself sparse, implying that there is much sparsity to be exploited in the intermediate computations. As discussed above, every intermediate directional gradient vector is at least as sparse as (and often much sparser than) the final Jacobian.

C.4 Usage of SparsLinC Access Routines

This section outlines the SparsLinC access routines and their use in the derivative code driver. These routines allow the user to set up and configure SparsLinC, pass data to it, and extract results and performance measures from it.

C.4.1 About SparsLinC 1.1 Routines and Their Names

SparsLinC provides multiprecision arithmetic support, meaning that the underlying vectors can be represented in REAL, DOUBLE PRECISION, COMPLEX, or DOUBLE COMPLEX precision. The routines involving a vector or vectors have a prefix letter designating the "precision" of the operation. For each precision-dependent SparsLinC routine, all instantiations of the routine have the same interface, meaning that they have the same arguments, in the same order, and with identical declarations except for the types of the vectors and multipliers (as an example, see the declaration of VALVEC in the definition of the [S,D,C,Z]SPSD routines in Section C.6).

Here is a summary of the naming conventions we have adopted for SparsLinC routines:

- The first letter will be an "S", "D", "C", "Z", or "X" indicating, respectively, whether the routine manipulates vectors in REAL, DOUBLE PRECISION, COMPLEX, or DOUBLE COMPLEX precision or whether it is a nonnumeric utility routine.
- The second and third letters will be "SP", to denote that the routine is in the SParsLinC library.
- The last two or three letters will be an abbreviation of the task performed by the routine.

We use the shorthand, "[S,D,C,Z] name" to refer to all four precision instantiations of a routine name.

C.4.2 Declaration of Sparse Variables

In Section C.2 we introduced the concept of directional gradient vectors. In the case of the non-sparse invocation of ADIFOR 2.0, these vectors are implemented as Fortran arrays. In the following examples in this and subsequent sections (C.4.2 - ??), assume that **x** is the independent variable

(i.e., all 1000 entries of \mathbf{x} are independent variables), \mathbf{f} is the dependent variable, and \mathbf{w} is an active variable we need to access in the derivative code driver:

```
REAL x(1000), f(5), w
```

In the nonsparse case, the derivative code generated by ADIFOR 2.0 (assuming the ADIFOR 2.0 options AD_PREFIX and AD_SEP have the default bindings of "g" and "_", respectively) will contain the following declarations:

```
REAL g_x(g_pmax_,1000), g_f(g_pmax_,5), g_w(g_pmax_)
```

By contrast, in the sparse case, the derivative code generated by ADIFOR 2.0 will contain the following declarations:

```
INTEGER g_x(1000), g_f(5), g_w
```

Note that the Fortran interface to SparsLinC declares each directional gradient vector to be an **INTEGER**. This is because each Fortran **INTEGER** gradient variable will be interpreted by SparsLinC to be a pointer to the sparse representation of the corresponding vector.

It is usually possible to clip-and-paste the declarations for the directional gradient vectors, and possibly the declarations of **COMMON** blocks that contain directional gradient vectors, from the code generated by ADIFOR 2.0. This is true for both nonsparse and sparse applications of ADIFOR 2.0. Just be aware that the declarations for the directional gradient vectors in the nonsparse and sparse codes are different.

Parenthetically, if you want to compare the sparse and nonsparse approaches for a particular problem, it is often good coding practice to write one driver for both, with preprocessor directives specifying the parts where the two differ. For example, for the above declaration, the following code could appear in the driver:

We use this format, wherever applicable (i.e., wherever corresponding sparse and nonsparse codes are present), in the rest of this discussion. (On most Unix systems, filenames ending with ".F" are interpreted by makefiles as Fortran files with preprocessor statements. Users unfamiliar with preprocessor directives can consult the "man" pages for "cpp", the C preprocessor.)

C.4.3 Initializing and Customizing SparsLinC

SparsLinC data structures must be initialized before any computation can be performed. To this end, the user *must* call the routine XSPINI before all other calls to any SparsLinC (except for calls to XSPCNF, which must precede the call to XSPINI, as described below) or ADIFOR 2.0-generated routines. XSPINI takes no arguments and is called as follows:

CALL XSPINI

The routine XSPCNF provides a means of tuning SparsLinC data structures for a particular problem at hand. Most sparse vectors maintained by SparsLinC are stored in what is commonly referred to as the "single subscript" and "compressed subscript" scheme. The single subscript scheme is the one already introduced in the Fortran context in Section C.1. In the compressed subscript scheme, in contrast, we keep track of nonzero index ranges. Thus the compressed subscript representation of the vector of Section C.1 would be as follows:

Index Array:	[1,1]	[3,4]	[7,7]	
Value Array:	11.0	33.0	44.0	77.0

This representation is more efficient than the single-subscript representation when sparse vectors contain a good portion of contiguous nonzero index ranges. A contiguous nonzero index range is a range of indices wherein all the corresponding values are nonzeros. For example, for our vector above, the largest such range has size 2 and contains elements 3 and 4. This scenario commonly arises when computing Jacobians with banded structure or gradients of partially separable functions. SparsLinC automatically converts a vector from the single-subscript to the compressed-subscript representation when the number of nonzeros in the vector exceeds a certain threshold, called switch_threshold, say.

For either representation, since the size to which vectors can grow is not known a priori, SparsLinC must provide, for the value and index arrays, a data structure capable of representing vectors of arbitrary size. The data structure currently employed in SparsLinC is a linked list of arrays each of which has a fixed number of entries. Let us denote this number of entries with SSbucket_size for the single subscript scheme and CSbucket_size for the compressed subscript scheme.

SparsLinC allows the user to adjust these values using the XSPCNF routine. For example, the sequence of calls

```
CALL XSPCNF(1,10)
CALL XSPCNF(2,500)
CALL XSPCNF(3,20)
```

sets SSbucket_size to 10, CSbucket_size to 500, and switch_threshold to 20. This would be appropriate, for example, for computing the gradient of a partially separable function (see Section C.3.2), where each ∇f_i usually contains about 20 nonzeros, and the number of independent variables is greater than 500.

While XSPINI assigns default values to these parameters and hence there is, from a functional perspective, no need to call XSPCNF, we encourage experimenting with these parameters and welcome feedback. Our experiments have shown that SparsLinC performs best if CSbucket_size is close in value to the size of the largest contiguous nonzero index range present in the problem. The tradeoff is between runtime and memory, where a larger value of CSbucket_size is likely to result in faster runtime, but also the dynamic allocation of more memory. In all cases, SSbucket_size should be set smaller (and usually much smaller) than CSbucket_size and should not exceed switch_threshold. We are working on a facility to trace and assimilate SparsLinC runtime information to aid with SparsLinC performance tuning.

The user should pay heed to the following important note: XSPCNF may be called only before calling XSPINI to set SSbucket_size and CSbucket_size. This is because once XSPINI is called, the array dimensions set via these options cannot be modified. Calling XSPCNF to set SSbucket_size and CSbucket_size, after a call to XSPINI, will result in a runtime error. Calls to XSPCNF to set switch_threshold can be made at any time.

C.4.4 Initializing the Seed Matrix

Each of the precision-specific SparsLinC routines [S, D, C, Z]SPSD converts a precision-specific sparse vector stored in the Fortran Sparse Format into a corresponding vector in the SparsLinC Sparse Format. In the following example, for the purpose of demonstration, we initialize columns 19 and 20 of g_x (corresponding to the derivatives of x(19) and x(20)), in both the nonsparse and sparse ways (assume that the arrays, INDVEC and VALVEC are declared appropriately):

```
#ifdef NON_SPARSE
    g_x(7,19) = 2.0
    g_x(19,19) = 1.0
    g_x(20,20) = 1.0
#elif SPARSE
    INDVEC(1) = 7
    VALVEC(1) = 2.0
    INDVEC(2) = 19
    VALVEC(2) = 1.0
    CALL SSPSD(g_x(19),INDVEC,VALVEC,2)
    CALL SSPSD(g_x(20),20,1.0,1)
#endif
```

```
Note also that a vector must be initialized in a "one-shot" fashion; hence, for example, the following piece meal approach would be an <u>incorrect</u> initialization of g_x(19):
```

```
INDVEC(1) = 7
VALVEC(1) = 2.0
CALL SSPSD(g_x(19), INDVEC, VALVEC, 1)
INDVEC(1) = 19
VALVEC(1) = 1.0
CALL SSPSD(g_x(19), INDVEC, VALVEC, 1)
```

Because of the "destructive copy" feature of SPSD (see Section C.6), the above would be equivalent to having made only the second of the two calls.

C.4.5 Extracting Directional Gradient Vectors from SparsLinC

SparsLinC provides two sets of precision-specific interfaces for extracting vector results:

[S,D,C,Z]SPXDQ (XVEC, INLEN, VPTR, OUTLEN, INFO)

extracts sparse_object(VPTR) into the Fortran Nonsparse Format vector XVEC. INLEN is the size of XVEC. The returned value OUTLEN is the largest index in the nonzero index set in sparse_object(VPTR). The value of INFO is used to indicate whether XVEC was sufficiently large to store all of the nonzero elements in sparse_object(VPTR). If OUTLEN is less than INLEN, then XVEC(OUTLEN+1:INLEN) is set to zero.

```
[S,D,C,Z]SPXSQ (INDVEC, VALVEC, INLEN, VPTR, OUTLEN, INFO)
```

extracts sparse_object(VPTR) into the Fortran Sparse Format vector represented by the two arrays INDVEC and VALVEC. INLEN is the size of the arrays INDVEC and VALVEC. The returned value OUTLEN is the number of nonzeros in sparse_object(VPTR). The value of INFO is used to indicate whether XVEC was sufficiently large to store all of the nonzero elements in sparse_object(VPTR). If OUTLEN is less than INLEN, then VALVEC(OUTLEN+1:INLEN) and INDVEC(OUTLEN+1:INLEN) are not referenced.

In the following code segments, we show examples of the usage of these extraction routines along with the corresponding necessary declarations (there is no equivalent ADIFOR 2.0 nonsparse extraction, since in that case the output variables are already in Fortran Nonsparse Format).

SPXDQ Example

```
PARAMETER (in_len_xd = g_pmax_)
INTEGER out_len_xd(5), info_xd(5)
REAL g_f_xd(in_len_xd,5)
. . .
DO i = 1, 5
  CALL SSPXDQ(g_f_xd(1,i), in_len_xd, g_f(i),
             out_len_xd(i), info_xd(i))
ENDDO
```

in_len_xd is a user-defined value specifying the leading dimension of the Fortran nonsparse column vectors of g_{f_xd} , i.e., it is the user's estimate of what is the largest index corresponding to a nonzero value in the vector to be extracted. In this case, by setting in_len_xd = g_pmax_, we have ensured ourselves that the SparsLinC Sparse Format vector will always "fit" into the Fortran Nonsparse Format vector. (In the next example we will discuss the case of underestimating memory requirements.)

Note that as specified above, **g_f_xd** is defined identically to the nonsparse **g_f** in Section C.4.2. Given Fortran's column order array storage, the above call to SSPXDQ causes g_f_xd to be aligned exactly with the nonsparse g_f .

SPXSQ Example

```
PARAMETER (in_len_xs = 40)
INTEGER g_f_ind_xs(in_len_xs,5), out_len_xs(5), info_xs(5)
REAL g_f_val_xs(in_len_xs,5)
. . .
DO i = 1, 5
  CALL SSPXSQ(g_f_ind_xs(1,i), g_f_val_xs(1,i), in_len_xs, g_f(i),
             out_len_xs(i), info_xs(i))
ENDDO
```

Here, our choice of in_len_xs = 40 implies that we have made the assumption that there are at most 40 nonzeros in any row of the Jacobian $\frac{\partial f}{\partial x}$ (i.e., given our declaration of x in Section C.4.2, we assume that the least sparse directional derivative vector is 96% sparse). To make sure that our memory requirement assumption holds, we add the following code:

```
max_len_xs = 0
DO i = 1, 5
  IF (info_xs(i) .NE. 0 .AND. out_len_xs(i) .GT. max_len_xs) THEN
    max_len_xs = out_len_xs(i)
  END IF
ENDDO
```

Now max_len_xs is encoded with the information we need. That is, if zero, our assumption was true, else, max_len_xs is equal to the true number of nonzeros in the least sparse row of the Jacobian and we know how much memory is really needed to extract all nonzero derivative values.

C.4.6 Adding the Contents of a Sparse Vector to a Dense Vector

Two SparsLinC routines are provided for adding a SparsLinC Sparse Format vector to a Fortran Nonsparse Format vector.

[S,D,C,Z]SPXMQ (XVEC, INLEN, MULT, VPTR, OUTLEN, INFO)

adds to XVEC the contents of sparse_object(VPTR) multiplied by MULT (i.e., XVEC = XVEC + MULT * sparse_object(VPTR)).

[S,D,C,Z]SPXAQ (XVEC, INLEN, VPTR, OUTLEN, INFO)

is identical to SPXMQ, except that the multiplier is assumed to be one (i.e., $XVEC = XVEC + sparse_object(VPTR)$). Note that SPXMQ and SPXAQ are functionally very similar to the SPXDQ routine, the only difference being that SPXDQ "assigns to" XVEC while SPXMQ and SPXAQ "add to" XVEC the contents of the sparse vector. Note also, that the interfaces of SPXAQ and SPXAQ are identical.

C.4.7 Dumping the Contents of a Sparse Vector

SparsLinC provides a set of precision-specific interfaces for dumping a sparse vector to a file.

[S,D,C,Z]SPPRQ (VPTR, EXT)

writes the number of nonzeros as well as index/value pairs of sparse_object(VPTR) to stdout or a file. EXT is an INTEGER in the range [0,999] and specifies the destination of the output: if zero, output is written to stdout; otherwise, output is written to the file SPPRQ.EXT.

SPPRQ can be a useful routine during debugging, to quickly check the values of a derivative vector somewhere in the code. It also has the advantage of not requiring that the user provide memory in which to extract the nonzero values in the sparse vector.

Admittedly, the interface of SPPRQ is rather crude. This is because we have avoided passing string arguments, because of the inconsistency of the Fortran-to-C string-passing protocols on different platforms.

SPPRQ Example

```
DO i = 1, 2
CALL SPPRQ(g_f(i), 6)
ENDDO
```

The above code prints the nonzero derivative information in $g_f(1)$ and $g_f(2)$ into the file "SPPRQ.6" in the current directory. Assume that $g_f(1)$ and $g_f(2)$ contain 4 and 2 nonzero values, respectively. Then the following is an example of what might be the contents of "SPPRQ.6" subsequent to the execution of the above code:

```
Number of nonzeros = 4

Index Value

-----

4 -4.892400e-01

5 6.523200e+00

6 -1.630800e+00

188 -2.030000e+01

Number of nonzeros = 2
```

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Index Value ----- ----37 3.812800e+00 256 1.000000e+00

Note that the vectors are printed out in the order in which the corresponding SPPRQ was called, and there is no identification in the file denoting which set of numbers belong to which vector. This task is left to the user.

C.4.8 Extracting Performance Information

In addition to providing derivative information, SparsLinC can also provide information about its own performance. Because of the system-specific nature of timing routines, runtime measures, however, are best arrived at by enveloping the appropriate system calls around the call to the top level subroutine. For example:

```
CALL timer(t1)
CALL g_top_foo(x, g_x, ...)
CALL timer(t2)
t_elapsed = t2 - t1
```

The SparsLinC routine XSPMEM returns how many kilobytes of memory have been dynamically allocated in the process of computing derivatives:

REAL USEDKB ... CALL XSPMEM(USEDKB)

C.4.9 Freeing Dynamically Allocated Memory

The routine XSPFRA frees all dynamically allocated memory in SparsLinC. Freeing memory might be useful if after finishing the derivative computation, the user wishes to perform some further memory-intensive computation. There are no arguments, and the call is simply

CALL XSPFRA

XSPFRA has the effect of leaving "dangling pointers", meaning that the Fortran INTEGER gradient variables, which are interpreted by SparsLinC as pointers, will retain the values (addresses) they contained before XSPFRA was called. However, after the call to XSPFRA, the memory pointed to by these pointers will no longer be under SparsLinC control. Any attempt to use these variables as pointers (e.g., by using them as pointer arguments to some SparsLinC routine) will likely cause a segmentation fault. For this reason, no calls to any SparsLinC routine should be made after XSPFRA.

C.5 A Brief Tutorial Example

SparsLinC is designed to be easy to use. First, apply ADIFOR 2.0 to generate sparse derivative code by specifying AD_FLAVOR=sparse in your script file. Then, create a "Sparse" derivative code driver. The derivative code driver is a user-generated Fortran program that invokes the derivative code generated by ADIFOR 2.0. In general, the sparse derivative code driver is analogous to the nonsparse derivative code driver and differs from the latter in only a few places. The following is an

example derivative code driver, based on the code fragments shown throughout Section C.4:

```
PROGRAM DRIVER
       REAL x(1000), f(5), w
 #ifdef NON_SPARSE
       REAL g_x(g_pmax_,1000), g_f(g_pmax_,5), g_w(g_pmax_)
 #elif SPARSE
       INTEGER g_x(1000), g_f(5), g_w
       PARAMETER (in_len_xs = 40)
       INTEGER g_f_ind_xs(in_len_xs,5), out_len_xs(5), info_xs(5)
       REAL g_f_val_xs(in_len_xs,5)
       REAL USEDKB
 #endif
 CCC
       We assume some statements at this point initialize the independent
 CCC
       variables.
 #ifdef SPARSE
       Tuning of SparsLinC parameters (optional) and mandatory initialization
CCC
       CALL XSPCNF ( 1, 10 )
       CALL XSPCNF (2, 500)
       CALL XSPCNF (3, 20)
       CALL XSPINI
 #endif
 CCC
       Initializing the seed matrix as identity.
 #ifdef NON_SPARSE
       DO i=1,1000
          DO j=1,1000
             g_x(i,j) = 0.0d0
          ENDDO
          g_x(i,i) = 1.0d0
       ENDDO
 #elif SPARSE
       DO i=1,1000
          CALL SSPSD(g_x(i),i,1.d0,1)
       ENDDO
 #endif
 #ifdef NON_SPARSE
       CALL g_top_foo(g_p_, x, g_x, ldg_x, f, g_f, ldg_f,
      +
                      w, g_w, ldg_w, non_active_var)
 #elif SPARSE
       CALL g_top_foo(x, g_x, f, g_f, w, g_w, non_active_var)
 #endif
       CALL EHRPT
 #ifdef SPARSE
```

Taking a close look at the calls to the top level routine, g_top_foo , in the driver code, we note that the sparse call differs from the nonsparse call in that there is never a need to pass a leading dimension argument along with each gradient variable argument, and also in that there is no need to pass a value for $g_p_$, the runtime nonsparse directional gradient vector size. Note that, regardless of whether ADIFOR 2.0 is invoked in the sparse or nonsparse mode, it generates the same subroutine name (assuming the ADIFOR 2.0 options AD_PREFIX and AD_SEP had the same bindings on both cases).

Finally, link all the generated derivative code and your driver with the SparsLinC 1.1 as described at the beginning of this chapter.

C.6 Detailed Specification of Access Routines

This section contains the detailed description of the SparsLinC 1.1 access routines discussed in Section C.4.

We adopt the convention that for a Fortran INTEGER variable VPTR, acting as a pointer to a SparsLinC Sparse Format vector, the sparse derivative object pointed to by VPTR is called sparse_object(VPTR). Also, to save space, only the calling sequence for one particular floating-point precision is provided. SSPSD, DSPSD, CSPSD, ZSPSD

SUBROUTINE SSPSD (VPTR, INDVEC, VALVEC, LEN)

Purpose

Conversion of a vector in Fortran Sparse Format into a vector in SparsLinC Sparse Format. The Fortran Sparse Format vector is given by the two arrays, INDVEC(1:LEN) and VALVEC(1:LEN), representing the indices and values of a sparse vector x (say), respectively. x is copied into sparse_object(VPTR), which is the vector in SparsLinC Sparse Format. The indices in INDVEC need not be in any particular order (internally, SPSD performs an ascending order sort). However, INDVEC and VALVEC must be identically aligned. That is, if in the Fortran Nonsparse Format x has a nonzero entry at index i with value v, then for some J, the following must hold: INDVEC(J) = i and VALVEC(J) = v. SPSD performs a destructive copy. That is, if sparse_object(VPTR) had been previously allocated (via SPSD or as a result of being an output argument of some other SparsLinC routine), the previous information in sparse_object(VPTR) is lost, and the dynamically allocated memory where that information resided is deallocated.

Arguments

VPTR	(output) INTEGER Upon exit, sparse_object(VPTR) contains a copy of the sparse vector repre- sented by INDVEC and VALVEC.
INDVEC	(input) INTEGER array, dimension (LEN) Indices of the nonzero values of the sparse vector. (We assume that indices are \geq 1; therefore, INDVEC entries \leq 0 would be incorrect and would result in a runtime error.)
VALVEC	(input) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] array, dimension (LEN) Nonzero values of the sparse vector.
LEN	(input) INTEGER LEN ≥ 0 is the number of nonzeros in the sparse vector. If LEN = 0, VPTR is initialized to point to the vector of all zeros and INDVEC and VALVEC are not referenced.

SSPXDQ, DSPXDQ, CSPXDQ, ZSPXDQ

SUBROUTINE SSPXDQ (XVEC, INLEN, VPTR, OUTLEN, INFO)

Purpose

Extracts sparse_object(VPTR) into the Fortran Nonsparse Format vector XVEC.

Arguments

XVEC	(output) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] array, dimension (INLEN) On exit, if INFO = 0, XVEC(1:INLEN) will contain a dense representation of sparse_object(VPTR). If OUTLEN < INLEN, then XVEC(OUTLEN+1:INLEN) is initialized to all zeros. If INFO \neq 0, XVEC is not referenced.
INLEN	(input) INTEGER

Length of XVEC.

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VPTR	(input/output) INTEGER Pointer to the SparsLinC Sparse Format vector. If VPTR equal initialized to point to the vector of all zeros (which is why it output argument).	
OUTLEN	(output) INTEGER Largest index in the nonzero index set in sparse_object(VPTR) will always be returned, whether XVEC is initialized or not. See tion of INFO below.	
INFO	(output) INTEGER If INLEN < OUTLEN, INFO will be set to -1, and XVEC is not Otherwise, INFO is set to 0, and XVEC(1:INLEN) is initialized Nonsparse Format copy of sparse_object(VPTR).	

SSPXSQ, DSPXSQ, CSPXSQ, ZSPXSQ

SUBROUTINE SSPXSQ (INDVEC, VALVEC, INLEN, VPTR, OUTLEN, INFO)

Purpose

<code>Extracts sparse_object(VPTR)</code> into the Fortran Sparse Format vector represented by the two arrays, <code>INDVEC</code> and <code>VALVEC</code>.

Arguments

INDVEC	(output) INTEGER array, dimension (INLEN) On exit, if INFO = 0, INDVEC(1:OUTLEN) contains the indices of the nonzero entries of sparse_object(VPTR). If INFO = 0 and OUTLEN < INLEN then INDVEC(OUTLEN+1:INLEN) is not referenced. If INFO \neq 0, INDVEC is not referenced.
VALVEC	(output) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] array, dimension (INLEN) On exit, if INFO = 0, VALVEC(1:OUTLEN) will contain the nonzero entries of sparse_object(VPTR). If INFO = 0 and OUTLEN < INLEN then VALVEC(OUTLEN+1:INLEN) is not referenced. If INFO \neq 0, VALVEC is not referenced.
INLEN	(input) INTEGER Length of INDVEC and VALVEC.
VPTR	(input/output) INTEGER Pointer to the SparsLinC Sparse Format vector. If VPTR equals NULL, it is initialized to point to the vector of all zeros (which is why it might be an output argument).
OUTLEN	(output) INTEGER Number of nonzeroes in sparse_object(VPTR). This value will always be re- turned, whether INDVEC and VALVEC are initialized or not. See the descrip- tion of INFO below.

INFO (output) INTEGER
If INLEN < OUTLEN, INFO will be set to -1, and INDVEC and VALVEC are
not referenced. Otherwise, INFO is set to 0, and INDVEC(1:OUTLEN) and
VALVEC(1:OUTLEN) are initialized to the Fortran Sparse Format copy of
sparse_object(VPTR).</pre>

SSPXMQ, DSPXMQ, CSPXMQ, ZSPXMQ

SUBROUTINE SSPXMQ (XVEC, INLEN, MULT, VPTR, OUTLEN, INFO)

Purpose

Adds the weighted contents of sparse_object(VPTR) to the Fortran Nonsparse Format vector XVEC, with MULT being the multiplicative weight (i.e., XVEC = XVEC + MULT * sparse_object(VPTR)). For example, say XVEC is a vector of length 7 containing all ones, MULT = 2.0, and sparse_object(VPTR) is as follows:

Index Array:	1	3	4	7
Value Array:	11.0	33.0	44.0	77.0

Subsequent to the call to this routine, XVEC would contain the following:

(23.0, 1.0, 67.0, 89.0, 1.0, 1.0, 155.0)

Arguments

XVEC	(input/output) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] array, dimension (INLEN) On exit, if INFO = 0, XVEC(1:INLEN) will have added to it the weighted contributions of the values in sparse_object(VPTR), with MULT specifying the weight. If INFO \neq 0, XVEC is not modified.
INLEN	(input) INTEGER Length of XVEC.
MULT	(input) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] Multiplier.
VPTR	(input/output) INTEGER Pointer to the SparsLinC Sparse Format vector. If VPTR equals NULL, it is initialized to point to the vector of all zeros (which is why it might be an output argument).
OUTLEN	(output) INTEGER Largest index in the nonzero index set in sparse_object(VPTR). This value will always be returned, whether XVEC is modified or not. See the descrip- tion of INFO below.
INFO	(output) INTEGER If INLEN $< 0UTLEN$, INFO will be set to -1, and XVEC is not modified. Other- wise, INFO is set to 0, and XVEC(1:INLEN) is modified as described above.

SSPXAQ, DSPXAQ, CSPXAQ, ZSPXAQ

SUBROUTINE SSPXAQ (XVEC, INLEN, VPTR, OUTLEN, INFO)

Purpose

Adds the contents of sparse_object(VPTR) to the Fortran Nonsparse Format vector XVEC (i.e., $XVEC = XVEC + \text{sparse_object(VPTR)}$). (SPXA is identical to the SPXMQ routine with MULT = 1.0; see the documentation for SPXMQ.)

Arguments

XVEC	(input/output) REAL [DOUBLE PRECISION, COMPLEX, DOUBLE COMPLEX] array, dimension (INLEN) On exit, if INFO = 0, XVEC(1:INLEN) will have added to it the values in sparse_object(VPTR). If INFO \neq 0, XVEC is not modified.
INLEN	(input) INTEGER Length of XVEC.
VPTR	(input/output) INTEGER Pointer to the SparsLinC Sparse Format vector. If VPTR equals NULL, it is initialized to point to the vector of all zeros (which is why it might be an output argument).
OUTLEN	(output) INTEGER Largest index in the nonzero index set in sparse_object(VPTR). This value will always be returned, whether XVEC is modified or not. See the descrip- tion of INFO below.
INFO	(output) INTEGER If INLEN $< 0UTLEN$, INFO will be set to -1, and XVEC is not modified. Other- wise, INFO is set to 0, and XVEC(1:INLEN) is modified as described above.

SSPPRQ, DSPPRQ, CSPPRQ, ZSPPRQ

SUBROUTINE SSPPRQ (VPTR, EXT)

Purpose

Writes number of nonzeros as well as index/value pairs of sparse_object(VPTR) onto stdout or a file, with the following format:

Number	of nonzeros	=
	Index	Value

Arguments

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VPTR	(input/output) INTEGER Pointer to the SparsLinC Sparse Format vector. If VPTR equal initialized to point to the vector of all zeros (which is why it s output argument).	'
EXT	(input) INTEGER Must be in the range [0,999]. If $EXT = 0$, output written is to s erwise EXT is converted to its ASCII equivalent and used as th appended to the filename "SPPR." and output is written to the	ne extension

XSPCNF

SUBROUTINE XSPCNF (OPT, VAL)

Purpose

Allows user to customize SparsLinC for each run. The following table specifies for each parameter its name, option number, default value, and range of allowable values. "SS-bucket_size" and "CSbucket_size" are the number of entries per array in the linked list representation of a single-subscript and compressed-subscript vector respectively. For all vector linear combinations, if at the conclusion of the computation the left-hand-side vector has an SS representation and the number of its nonzero entries exceeds "switch_threshold", the vector is converted to a CS representation.

Name	<u>0PT</u>	$\underline{\text{Default}}$	Range
SSbucket_size	1	8	>1
CSbucket_size	2	32	>1
$switch_threshold$	3	16	>1

XSPCNF with OPT = 1 or OPT = 2 may be called only before calling XSPINI. Calling XSPCNF with OPT = 1 or 2 after a call to XSPINI will result in a runtime error. Calls to XSPCNF with OPT = 3 can be made at any time.

Arguments

OPT	(input) INTEGER Specifies the option number associated with a given parameter as given in the above table.
VAL	(input) INTEGER The new value for the parameter specified by OPT .

XSPMEM

SUBROUTINE XSPMEM (USEDKB)

Revision \mathbf{D}

Purpose

Reports how many kilobytes of memory have been allocated dynamically in SparsLinC.

Arguments

USED

(output) REAL. The number of kilobytes of storage allocated for SparsLinC data structures.

XSPINI

SUBROUTINE XSPINI

Purpose

Initializes the sparse data structures by dynamically allocating memory for some SparsLinCinternal global variables. It must be called before any of the other SparsLinC routines (except for calls to XSPCNF with OPTs 1-2) and needs to be called no more than once (when called more than once, all but the first call act as no-ops).

Arguments

none

XSPFRA

SUBROUTINE XSPFRA

Purpose

Frees all memory allocated for C sparse vector data structures. Note: all pointers to sparse directional gradient variables (VPTR's) are left dangling.

Arguments

none

Appendix D

Installation, Configuration and Use of ADIFOR 2.0 on Windows 95/NT

- D.1 Installation
- D.2 Configuration

D.3 Use

The use of ADIFOR 2.0 under Windows-95/NT is practically identical to its use under Unix - you first create a composition and an ADIFOR script file, then you invoke the ADIFOR Preprocessor which is named Adifor21 passing it the same options as previously, and then you link your code against the generated derivative code and against the ADIntrinsics and SparsLinC libraries. Note that the appropriate Windows 95/NT libraries and components are named ADIntrinsics.lib, ReqADIntrinsics.obj and SparsLinC.lib. For each of the examples that we have provided, you will find a script adANDrun.bat that can be used to invoke ADIFOR and then run the generated derivative code.

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